



# 5 Tips to minimize your Pass/Fail errors

<i>Technical Manager</i>
<i>Su Hyong Park</i>



# Agenda – what's next?

- ➔ • What is measurement decision risk?

# Why do you make measurements?



What do you do with the result after you take a measurement?

Do you compare your result to a [customer] specification and make a “Pass” or “Fail” decision to ship or reject the item under test?

# Why are decision rules important?

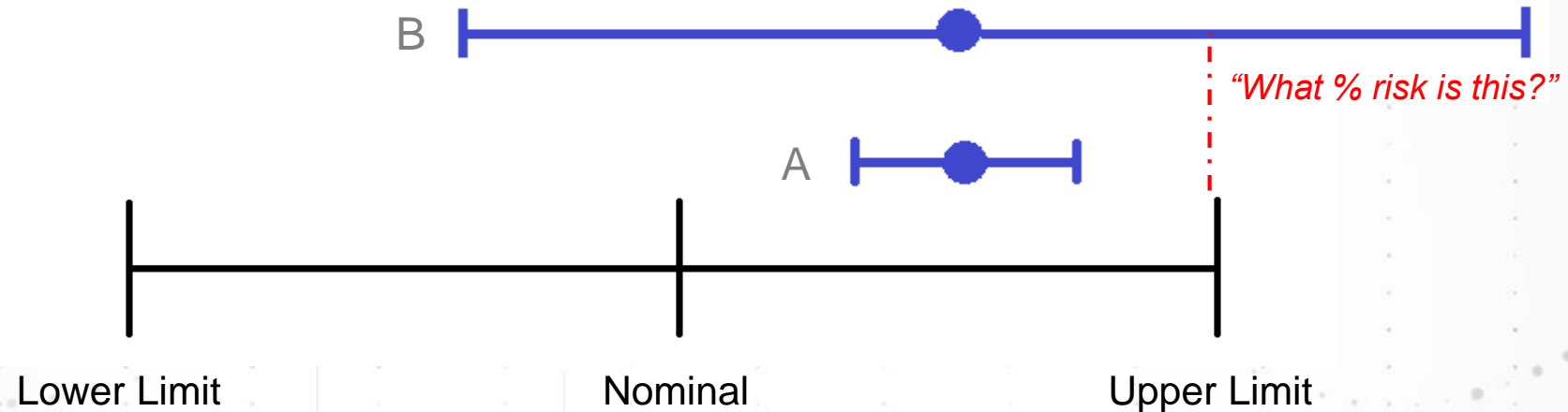
- When performing a measurement and subsequently making a Pass/Fail statement such as in or out-of-tolerance to manufacturer's specifications **there are two possible outcomes**
  - You are right
  - You are wrong
- Each measurement has an associated uncertainty, and it is that uncertainty that can affect your chance of being right or wrong



**There are no perfect measurements ☹️**

Source: Jeff Gust, Chief Corporate Metrologist, Fluke

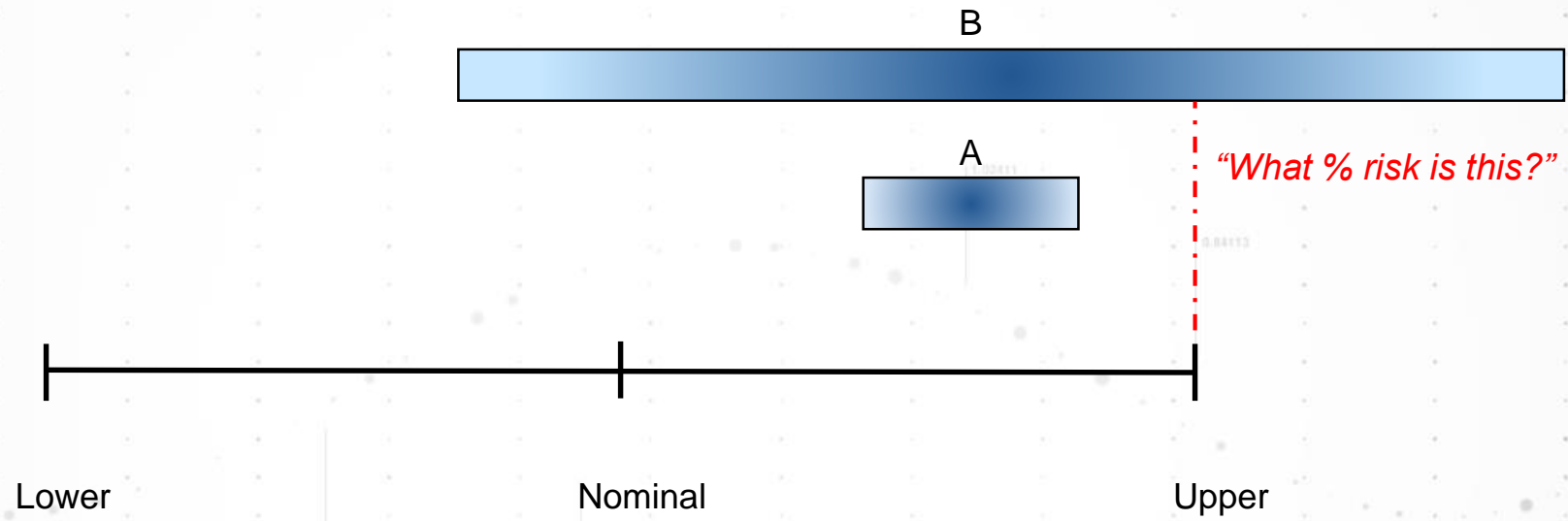
# Measurement Decision Risk



- If your uncertainty is large compared to the specified requirement, how confident are you in your declaration of In-Tolerance or Out-of-Tolerance?

Source: Jeff Gust, Chief Corporate Metrologist, Fluke

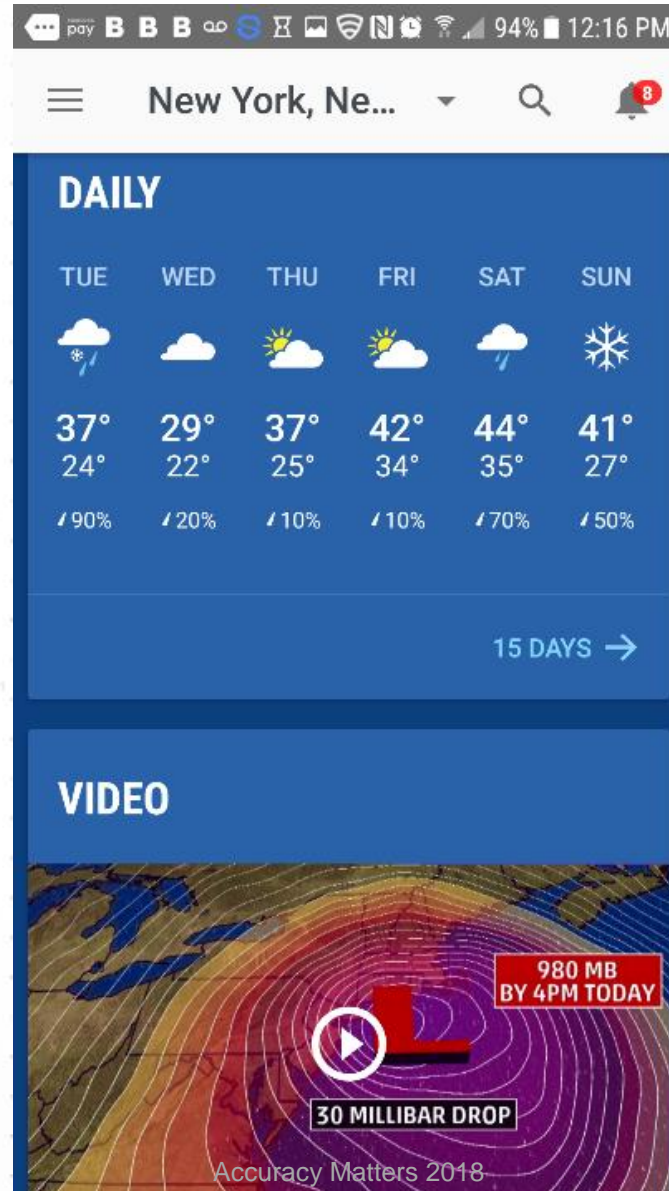
# What % Risk is This?



*Drawing courtesy of Steve Marschke, Raytheon*

# People Know How to Make Trade-offs Based on % Risk

What actions will  
you take each day?



# Agenda – what's next?



- What is measurement decision risk?



- Errors due to measurement decision risk



# Measurement Uncertainty Causes Two Types of Test Errors That Increase Testing Costs

		True State of Product	
		Good	Bad
Test Outcome	Pass		Increases return rate & warranty costs
	Fail	Increases rework & scrap costs	

# Agenda – what's next?

- What is measurement decision risk?
- Errors due to measurement decision risk
- ➔ • Measurement Uncertainty (a.k.a. “test system accuracy”)



# M3003

EDITION 3 | NOVEMBER 2012

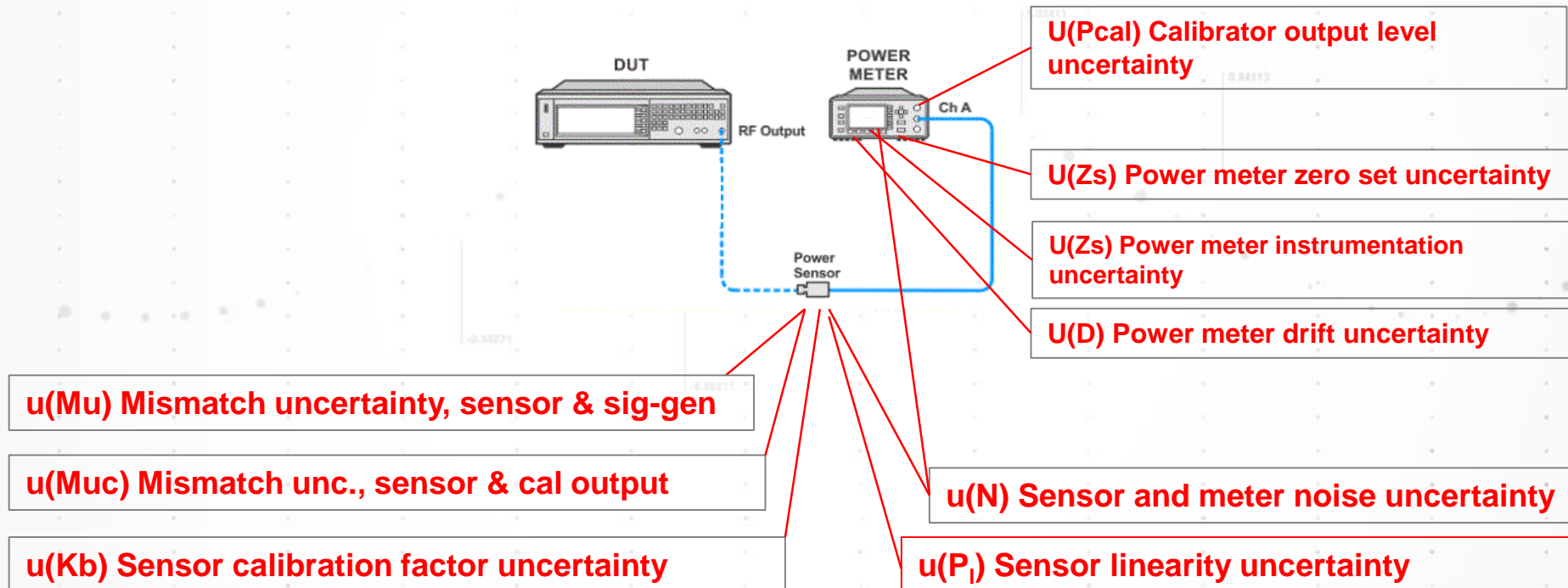
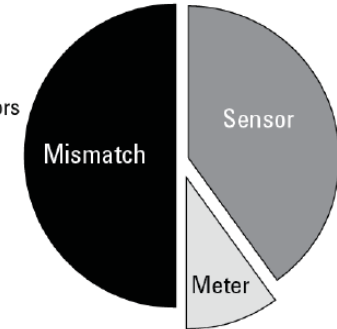
## The Expression of Uncertainty and Confidence in Measurement

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# Power Measurement Uncertainty

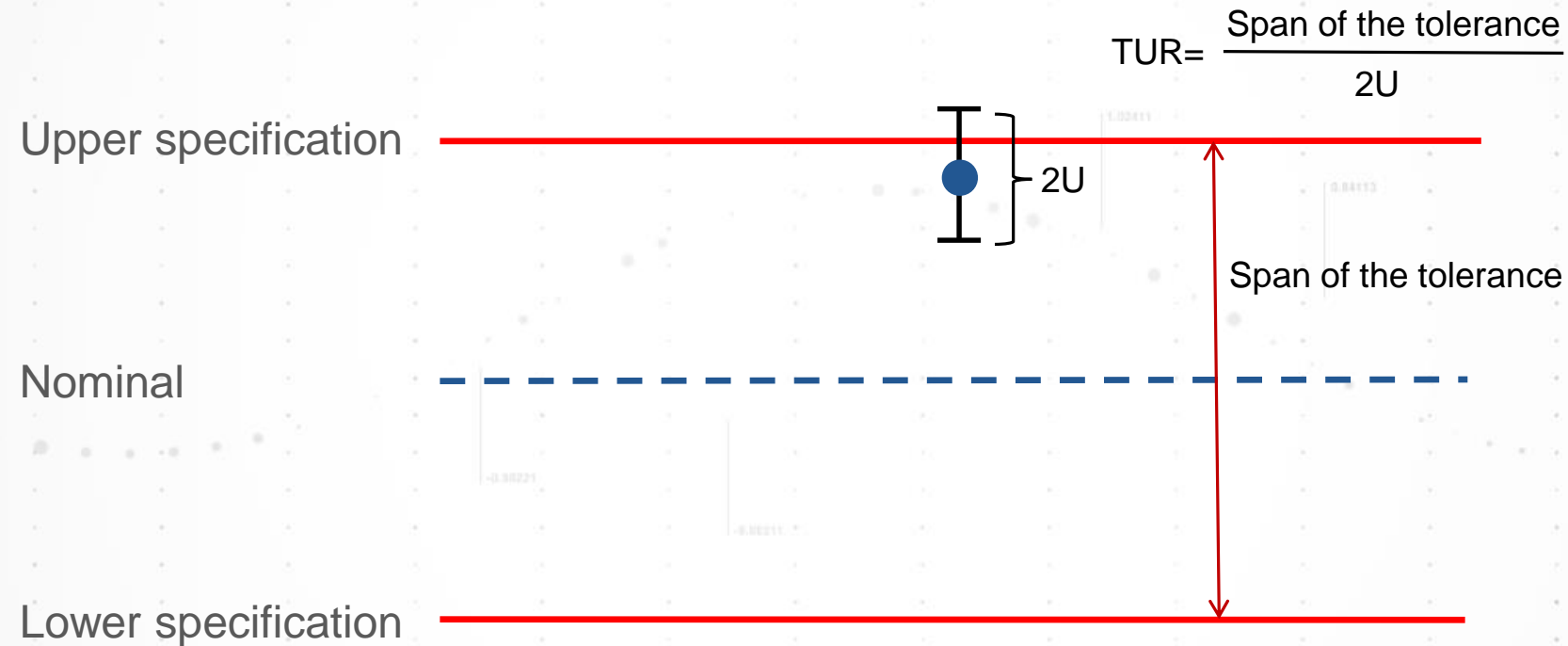
- Sensor and Source Mismatch Errors
- Power Sensor Errors
- Power Meter Errors



Application Note

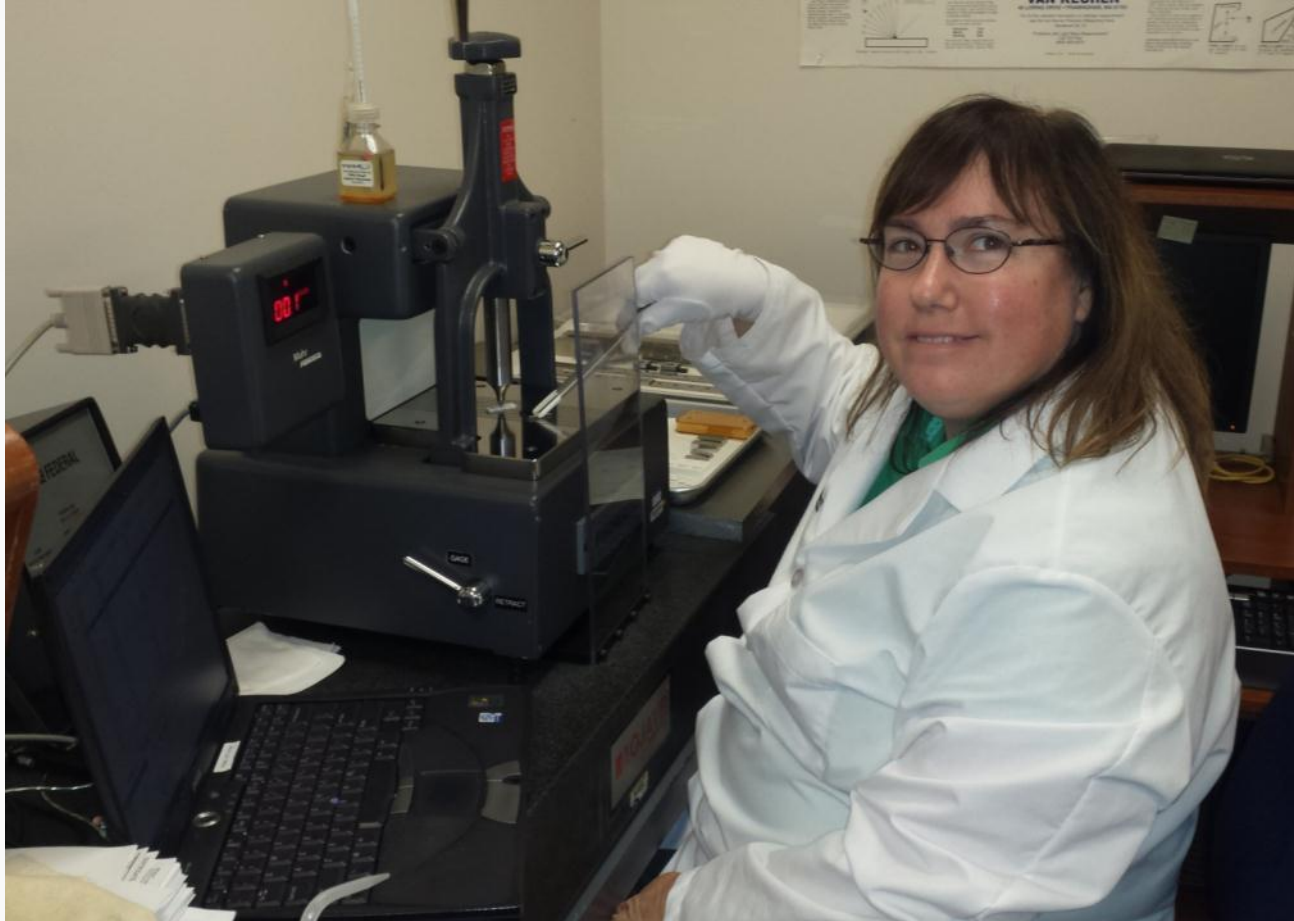
<http://cp.literature.keysight.com/litweb/pdf/5988-9215EN.pdf>

# Test Uncertainty Ratio (TUR) Defined



TUR = Test Uncertainty Ratio, paragraph 3.11 ANSI Z540.3

# When is TAR<sup>1</sup> acceptable?

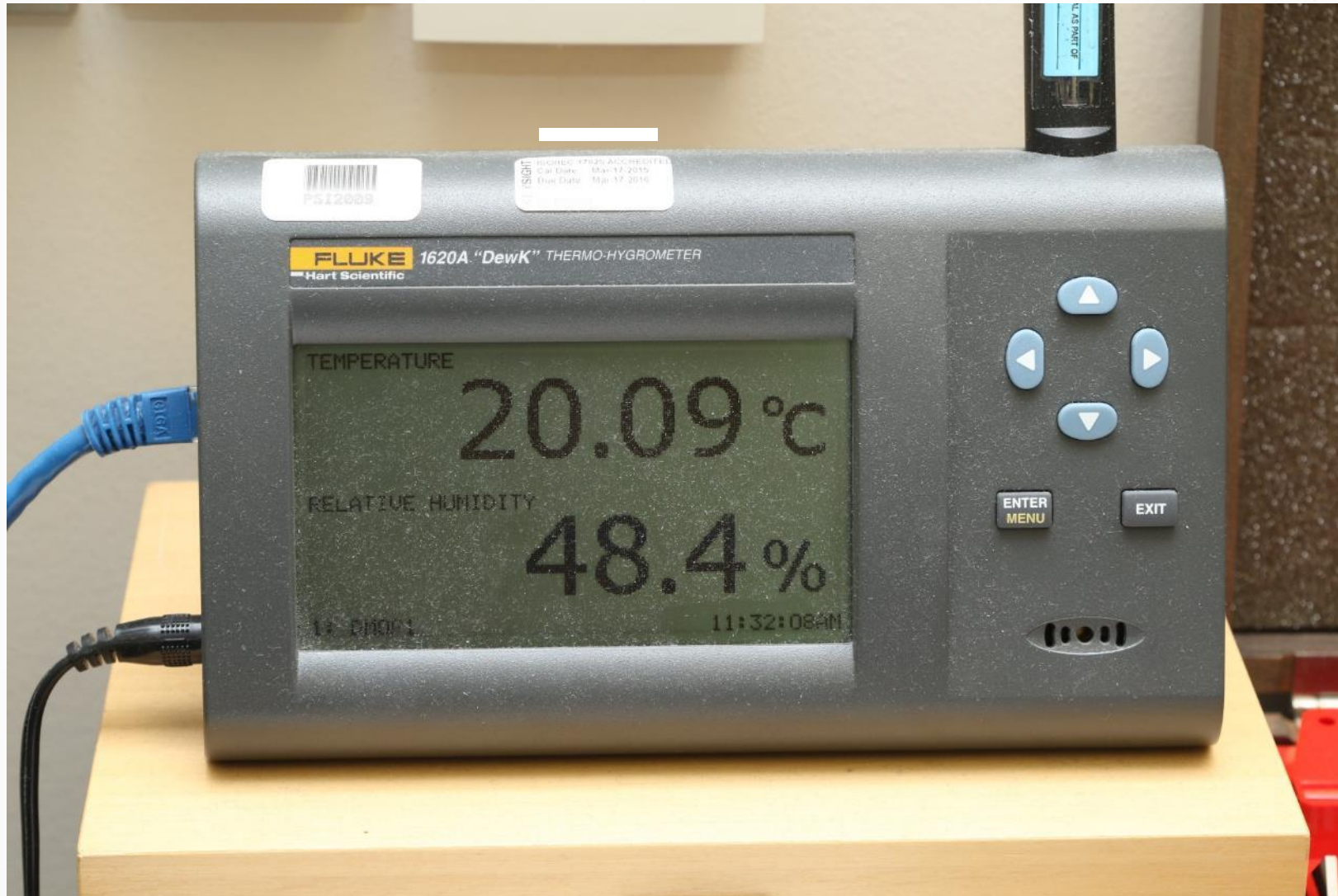


## Gage block comparator

1. TAR = "Test Accuracy Ratio", compares Tolerance to a single error type.



# Gage Blocks Need $20^{\circ} \pm 0.5^{\circ}$ Celsius





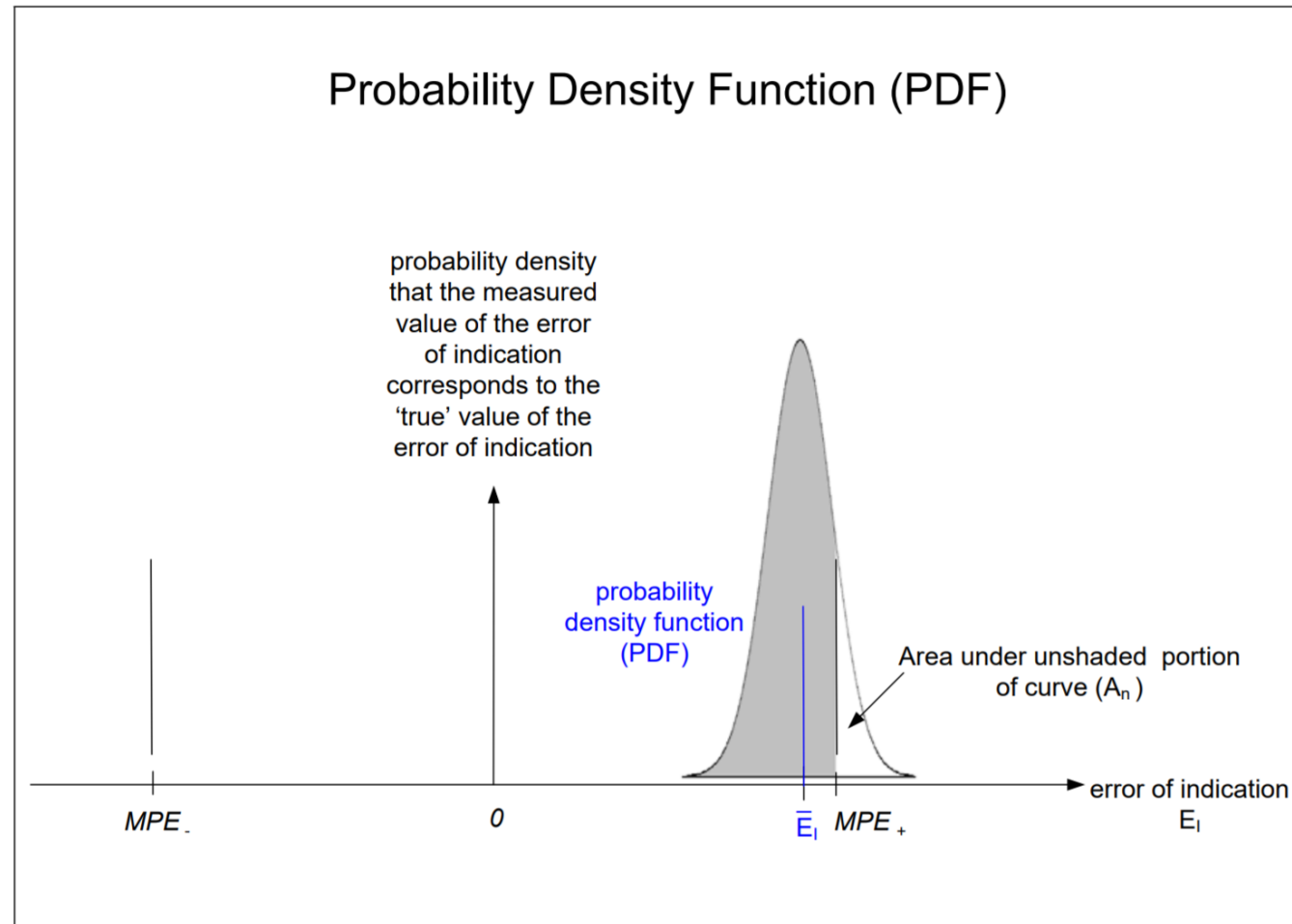


# Agenda – what's next?

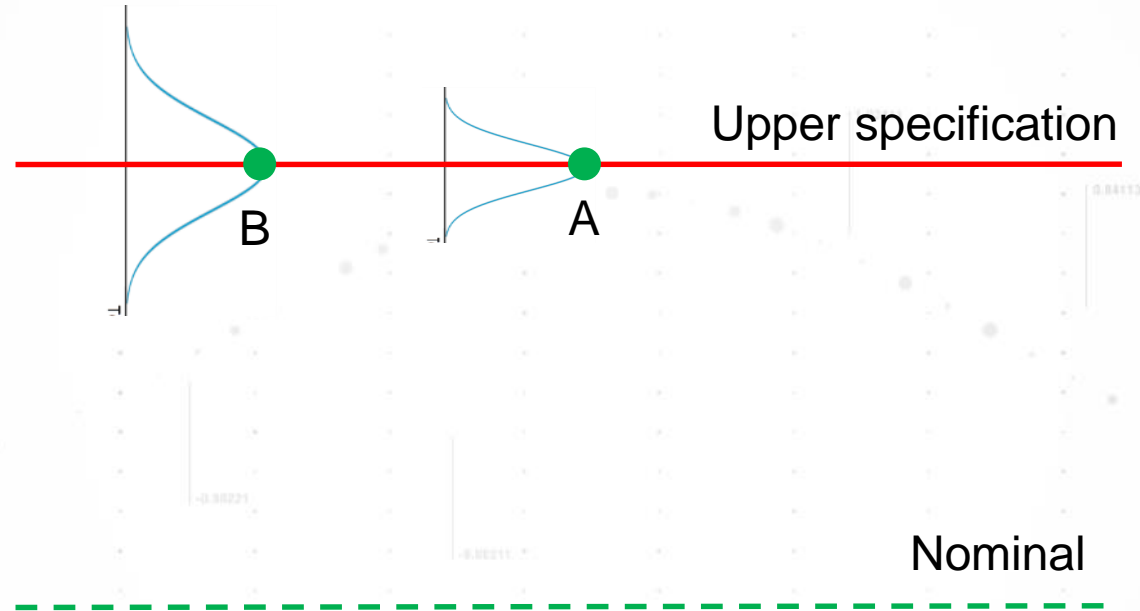
- What is measurement decision risk?
- Errors due to measurement decision risk
- Measurement Uncertainty (a.k.a system accuracy)
- ➔ • Specific risk

# Specific Risk

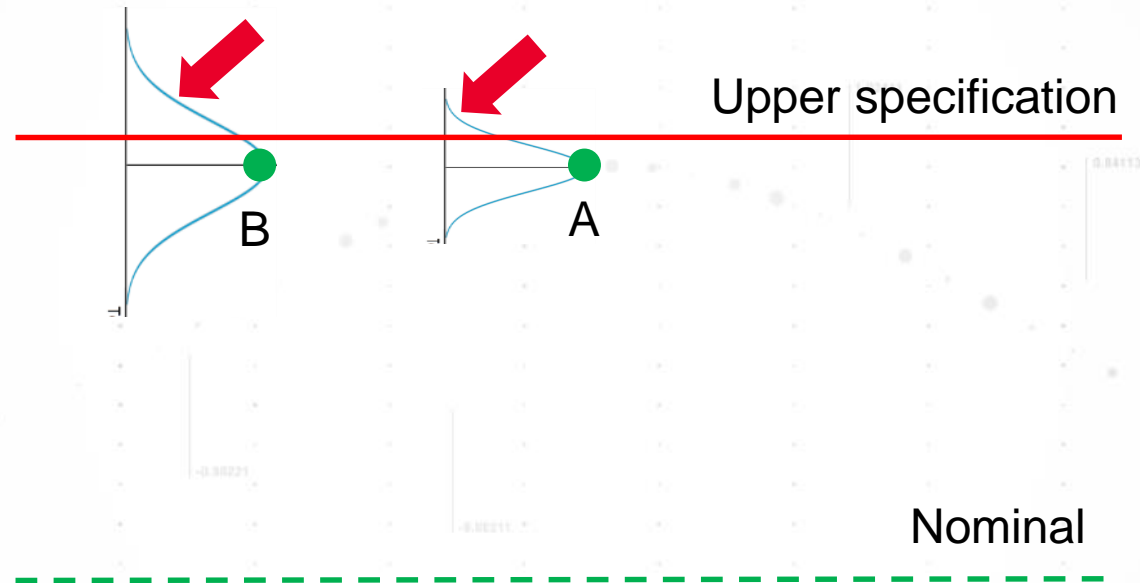
OIML G 19:2017 (E)



# Zero Guardband Decision Rule – “Shared risk”



# A Little Guard Band Goes a Long Way for Higher TURs



# Example: Estimating Specific PFA (2)

Standard normal distribution table

The table below contains the area under the standard normal curve from  $x = 0$  to a specified value  $x = \alpha$ .

Area under the Normal Curve from  $X = 0$  to  $X = \alpha$

$\alpha$	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.00000	0.00399	0.00798	0.01197	0.01595	0.01994	0.02392	0.02790	0.03188	0.03586
0.1	0.03983	0.04380	0.04776	0.05172	0.05567	0.05962	0.06356	0.06749	0.07142	0.07535
0.2	0.07926	0.08317	0.08706	0.09095	0.09483	0.09871	0.10257	0.10642	0.11026	0.11409
0.3	0.11791	0.12172	0.12552	0.12930	0.13307	0.13683	0.14058	0.14431	0.14803	0.15173
0.4	0.15542	0.15910	0.16276	0.16640	0.17003	0.17364	0.17724	0.18082	0.18439	0.18793
0.5	0.19146	0.19497	0.19847	0.20194	0.20540	0.20884	0.21226	0.21566	0.21904	0.22240
0.6	0.22575	0.22907	0.23237	0.23565	0.23891	0.24215	0.24537	0.24857	0.25175	0.25490
0.7	0.25804	0.26115	0.26424	0.26730	0.27035	0.27337	0.27637	0.27935	0.28230	0.28524
0.8	0.28814	0.29103	0.29389	0.29673	0.29955	0.30234	0.30511	0.30785	0.31057	0.31327
0.9	0.31594	0.31859	0.32121	0.32381	0.32639	0.32894	0.33147	0.33398	0.33646	0.33891
1.0	0.34134	0.34375	0.34614	0.34849	0.35083	0.35314	0.35543	0.35769	0.35993	0.36214
1.1	0.36433	0.36650	0.36864	0.37076	0.37286	0.37493	0.37698	0.37900	0.38100	0.38298
1.2	0.38493	0.38686	0.38877	0.39065	0.39251	0.39435	0.39617	0.39796	0.39973	0.40147
1.3	0.40320	0.40490	0.40658	0.40824	0.40988	0.41149	0.41308	0.41466	0.41621	0.41774
1.4	0.41924	0.42073	0.42220	0.42364	0.42507	0.42647	0.42785	0.42922	0.43056	0.43189
1.5	0.43319	0.43448	0.43574	0.43699	0.43822	0.43943	0.44062	0.44179	0.44295	0.44408
1.6	0.44520	0.44630	0.44738	0.44845	0.44950	0.45053	0.45154	0.45254	0.45352	0.45449
1.7	0.45543	0.45637	0.45728	0.45818	0.45907	0.45994	0.46080	0.46164	0.46246	0.46327
1.8	0.46407	0.46485	0.46562	0.46638	0.46712	0.46784	0.46856	0.46926	0.46995	0.47062
1.9	0.47128	0.47193	0.47257	0.47320	0.47381	0.47441	0.47500	0.47558	0.47615	0.47670
2.0	0.47725	0.47778	0.47831	0.47882	0.47932	0.47982	0.48030	0.48077	0.48124	0.48169
2.1	0.48214	0.48257	0.48300	0.48341	0.48382	0.48422	0.48461	0.48500	0.48537	0.48574
2.2	0.48610	0.48645	0.48679	0.48713	0.48745	0.48778	0.48809	0.48840	0.48870	0.48899
2.3	0.48928	0.48956	0.48983	0.49010	0.49036	0.49061	0.49086	0.49111	0.49134	0.49158
2.4	0.49180	0.49202	0.49224	0.49245	0.49266	0.49286	0.49305	0.49324	0.49343	0.49361
2.5	0.49379	0.49396	0.49413	0.49430	0.49446	0.49461	0.49477	0.49492	0.49506	0.49520
2.6	0.49534	0.49547	0.49560	0.49573	0.49585	0.49598	0.49609	0.49621	0.49632	0.49643
2.7	0.49653	0.49664	0.49674	0.49683	0.49693	0.49702	0.49711	0.49720	0.49728	0.49736
2.8	0.49744	0.49752	0.49760	0.49767	0.49774	0.49781	0.49788	0.49795	0.49801	0.49807
2.9	0.49813	0.49819	0.49825	0.49831	0.49836	0.49841	0.49846	0.49851	0.49856	0.49861
3.0	0.49865	0.49869	0.49874	0.49878	0.49882	0.49886	0.49889	0.49893	0.49896	0.49900
3.1	0.49903	0.49906	0.49910	0.49913	0.49916	0.49918	0.49921	0.49924	0.49926	0.49929
3.2	0.49931	0.49934	0.49936	0.49938	0.49940	0.49942	0.49944	0.49946	0.49948	0.49950
3.3	0.49952	0.49953	0.49955	0.49957	0.49958	0.49960	0.49961	0.49962	0.49964	0.49965
3.4	0.49966	0.49968	0.49969	0.49970	0.49971	0.49972	0.49973	0.49974	0.49975	0.49976
3.5	0.49977	0.49978	0.49978	0.49979	0.49980	0.49981	0.49981	0.49982	0.49983	0.49983
3.6	0.49984	0.49985	0.49985	0.49986	0.49986	0.49987	0.49987	0.49988	0.49988	0.49989
3.7	0.49989	0.49990	0.49990	0.49990	0.49991	0.49991	0.49992	0.49992	0.49992	0.49992
3.8	0.49993	0.49993	0.49993	0.49994	0.49994	0.49994	0.49994	0.49995	0.49995	0.49995
3.9	0.49995	0.49995	0.49996	0.49996	0.49996	0.49996	0.49996	0.49996	0.49997	0.49997

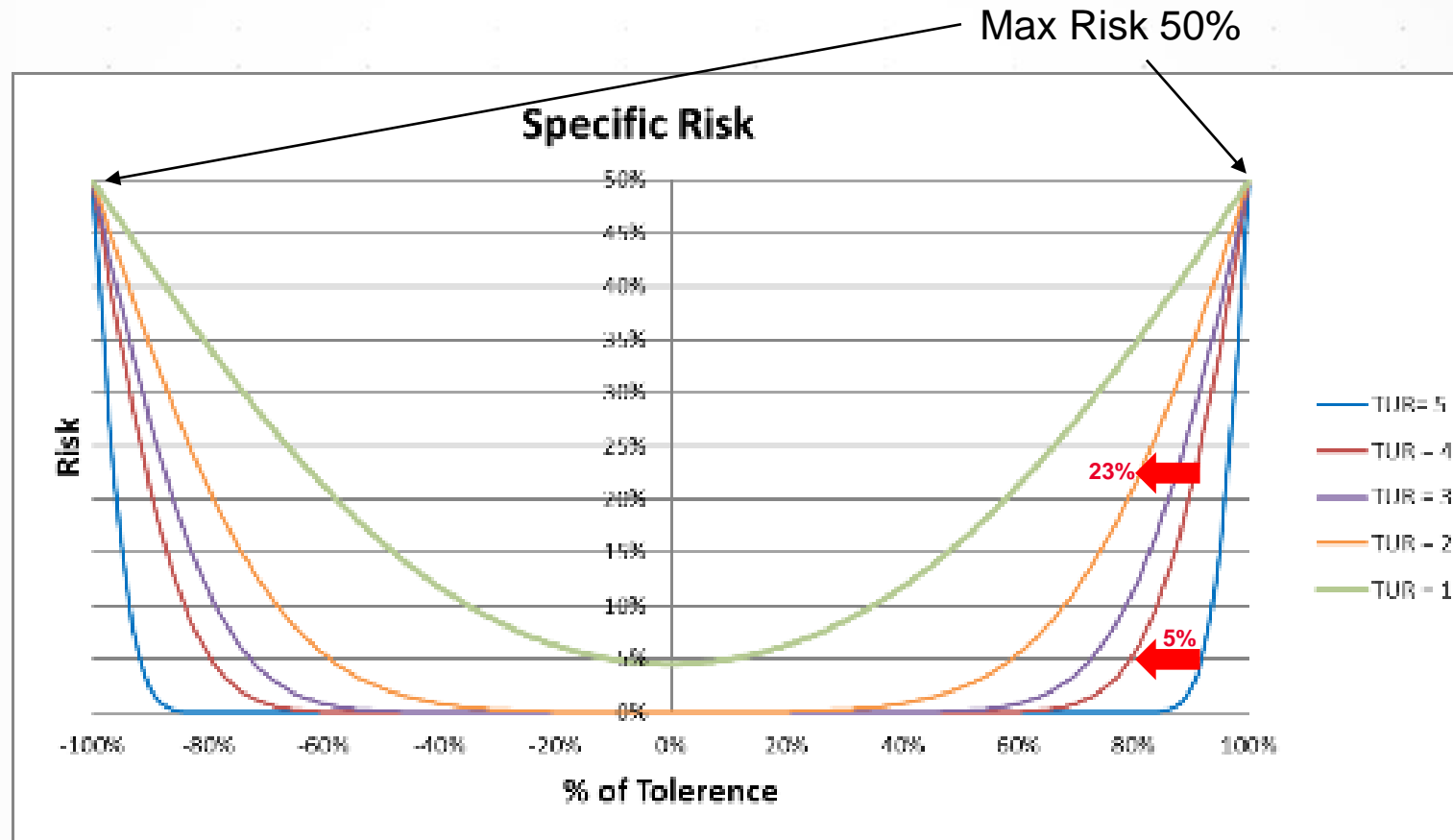
Source:

OIML G 19 Annex B; an adaptation from the  
NIST/SEMATECH e-Handbook of Statistical Methods

<http://www.itl.nist.gov/div898/handbook/eda/section3/eda3671.htm>

# Estimating Specific Measurement Decision Risk

IS A FUNCTION OF TOLERANCE, UNCERTAINTY, AND MEASURED VALUE



Source: Harben & Stern, NCSLI paper 2017



# Example: Speed Limit Enforcement




# Example : Speed Limit Enforcement



If the Doppler radar gun uncertainty = 2%,  
what speed must he measure to ensure a car is  
travelling > 100 km/hr (60 mph) with 99.9%  
probability?

One-sided specific risk

$p_c$	$\bar{p}_c$	$z$
0.80	0.20	0.84
0.90	0.10	1.28
0.95	0.05	1.64
0.99	0.01	2.33
<u>0.999</u>	0.001	<u>3.09</u>

  $v_{\max} = \frac{v_0}{1 - 0.02z} = \frac{100}{1 - 0.02 \times 3.09} \text{ km/h} \approx \underline{107 \text{ km/h.}}$

Source: Clause 8.3.3, ISO 15427



Meas. 85.3 mph to  
prove 80 mph @ 99.9%



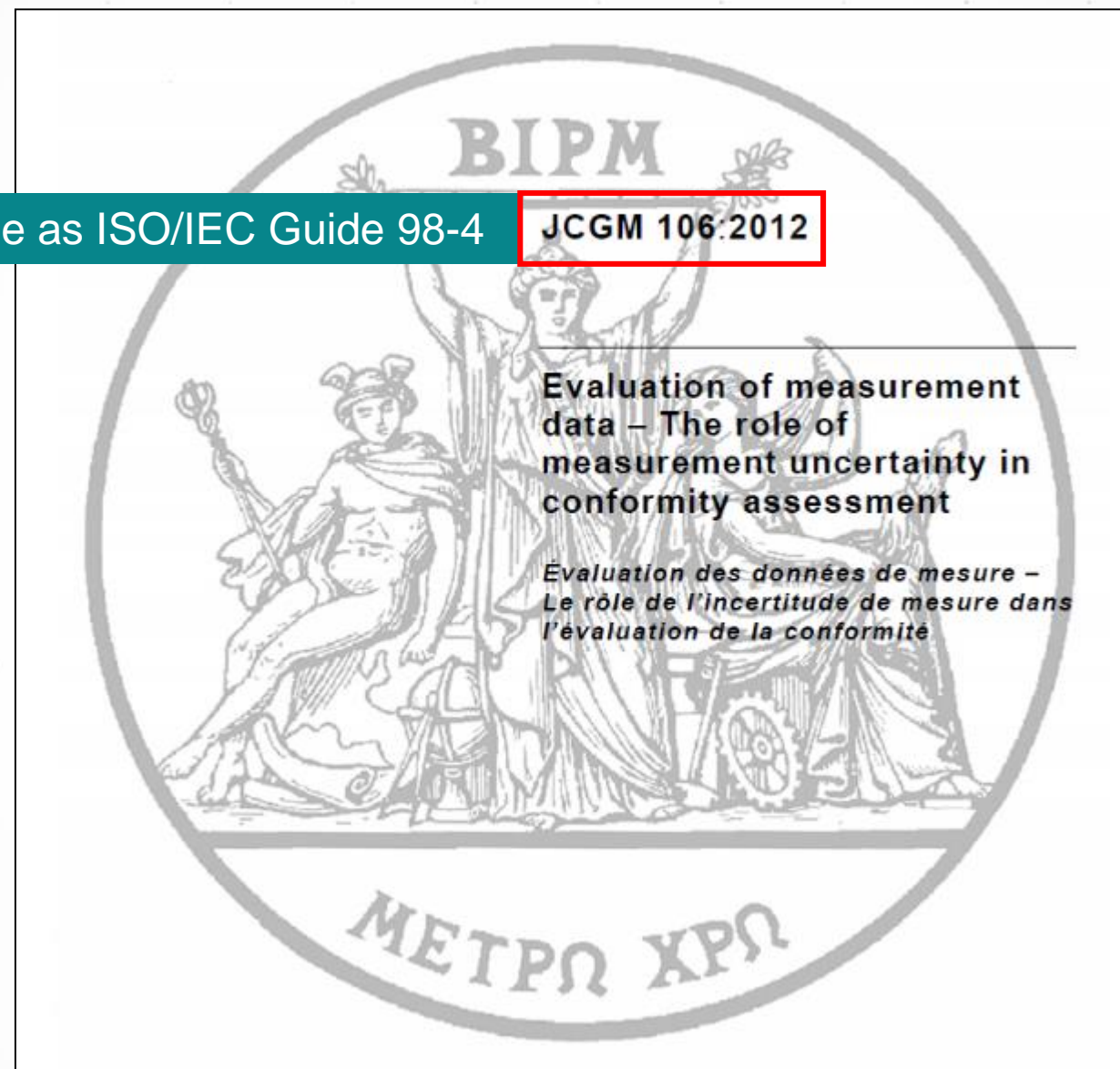
# Agenda – what's next?

- What is measurement decision risk?
- Errors due to measurement decision risk
- Measurement Uncertainty (a.k.a system accuracy)
- Specific risk
- ➔ • Average risk



Same as ISO/IEC Guide 98-4

JCGM 106:2012



# Understanding Measurement Risk

By: Michael Dobbert

2007 NCSL International Workshop and Symposium

## Understanding Measurement Risk

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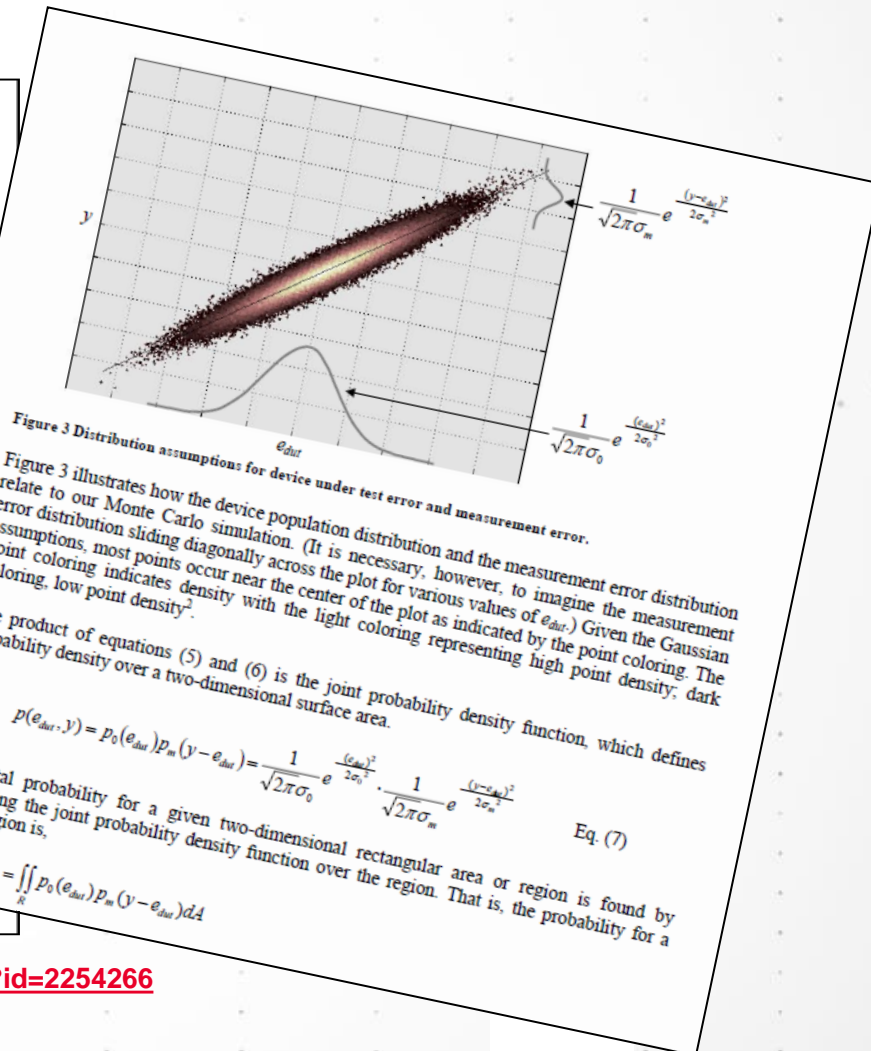
### 1 Abstract

One key reason for performing a calibration is to assess a device as either in- or out-of-tolerance. Common calibration test scenarios compare a device parameter against that of a measurement standard by way of a measurement process. If the difference between the device parameter and the measurement standard is greater than the specified tolerance, the device is deemed out-of-tolerance. However, errors in the measurement process bring about the possibility of an incorrect assessment. An incorrect assessment may result in devices incorrectly declared as in-tolerance (false-accept) or incorrectly declared as out-of-tolerance (false-reject).

The risk of making an incorrect in- or out-of-tolerance assessment can be determined by evaluating probability density functions that incorporate a device's parameter population and the measurement error. This paper provides an intuitive explanation of these probability density functions drawing on Monte Carlo simulation to demonstrate the relationship between a device's true value and the corresponding measured value.

### 2 Introduction

In manufacturing facilities throughout the world, test engineers design measurement procedures for manufacturing purposes. It is common for test engineers to rely on the specifications of



<http://literature.cdn.keysight.com/litweb/pdf/5991-1265EN.pdf?id=2254266>

# Joint Probability Density Function

$$p_0(e_{dut})p_m(y - e_{dut}) = \underbrace{\frac{1}{\sqrt{2\pi}\sigma_0} e^{-\frac{(e_{dut})^2}{2\sigma_0^2}}}_{\text{Device Population Error}} \times \underbrace{\frac{1}{\sqrt{2\pi}\sigma_m} e^{-\frac{(y-e_{dut})^2}{2\sigma_m^2}}}_{\text{Measurement Process Uncertainty}}$$



Device Population Error

Measurement Process Uncertainty

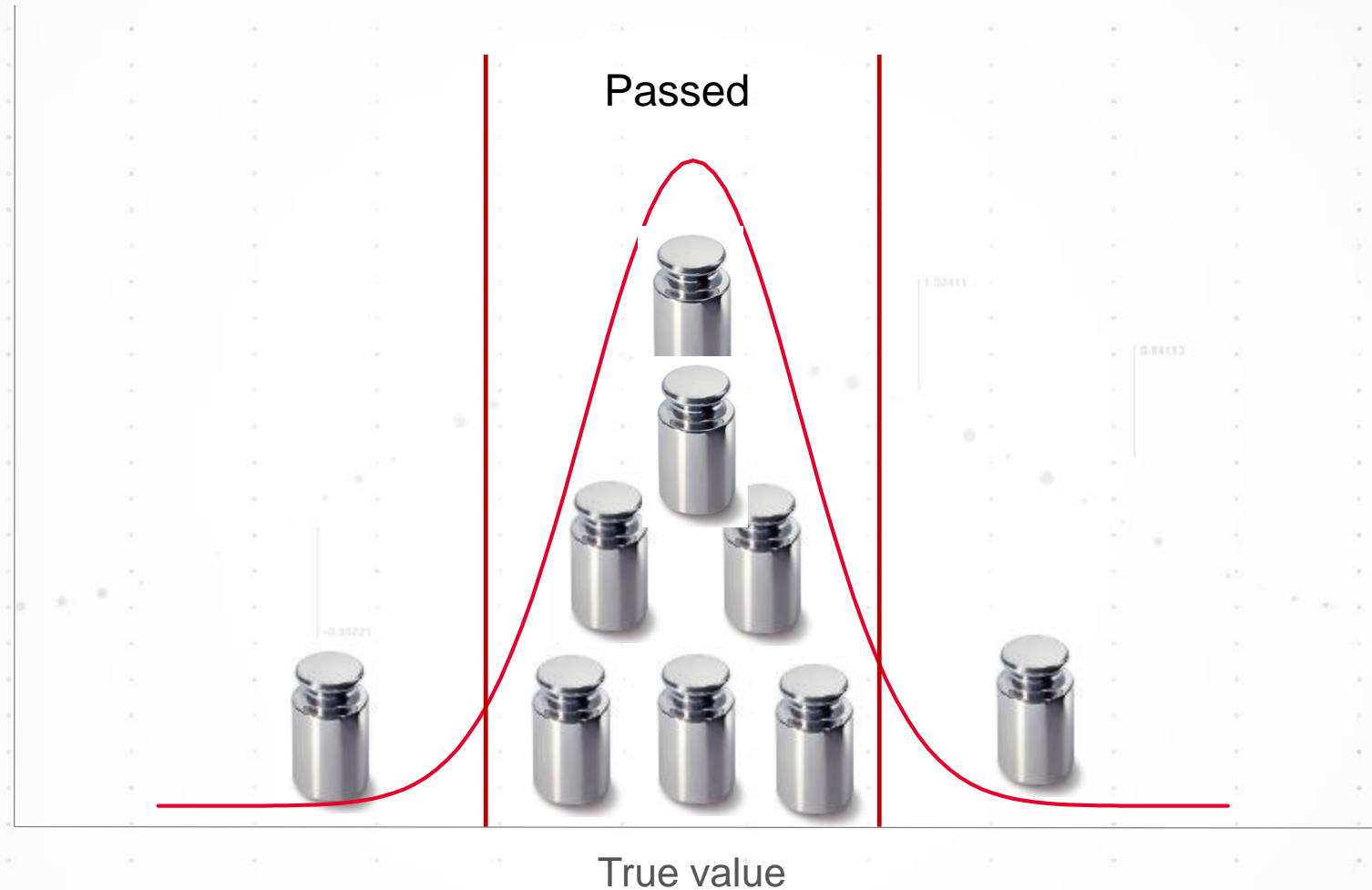
Global risk per clause 9.5,  
JCGM 106:2012

$$P_R = \iint_R p_0(e_{dut})p_m(y - e_{dut})dA$$



Error = Measured Value - True Value

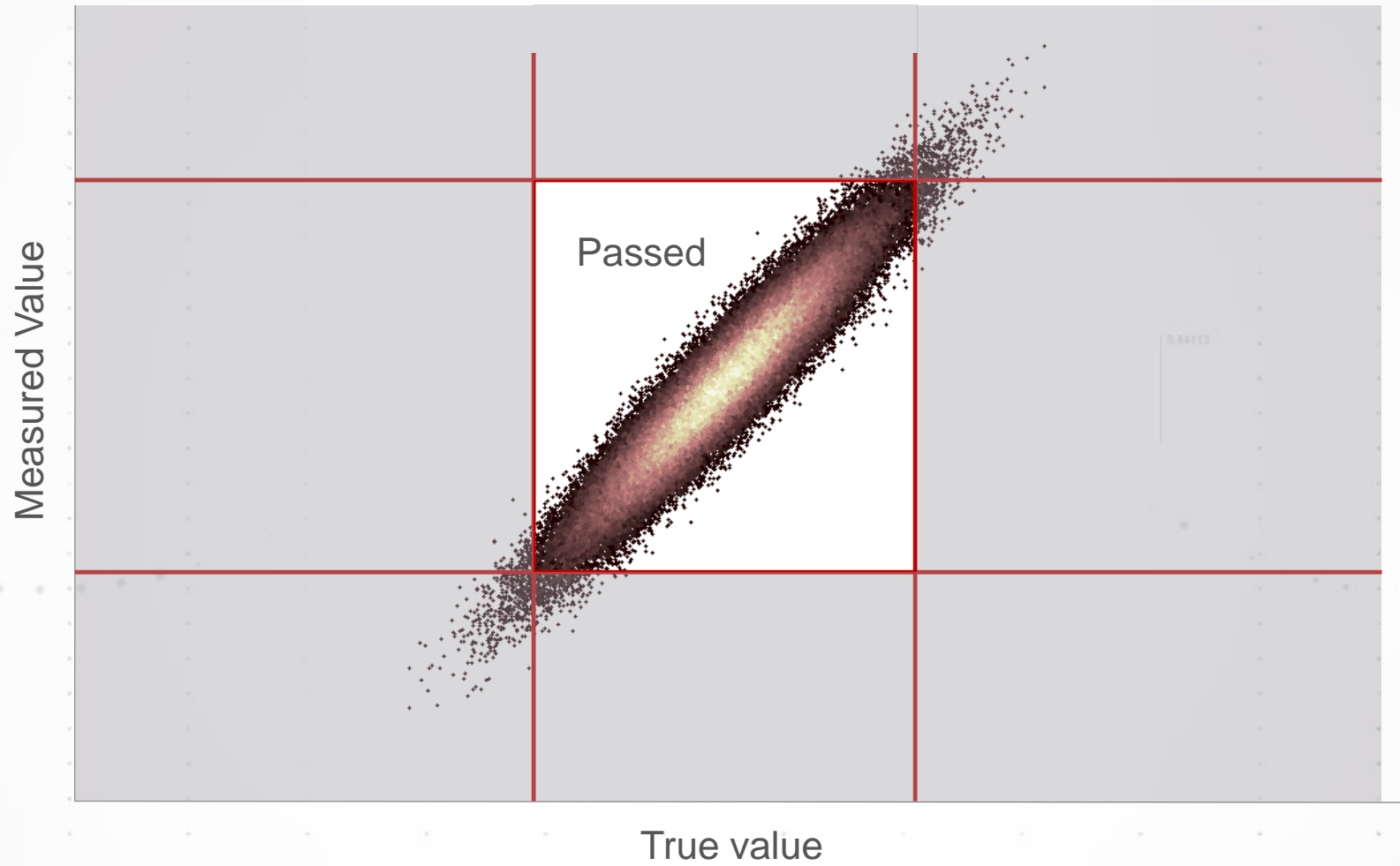
# Any Manufactured Item Has a Distribution of True Values



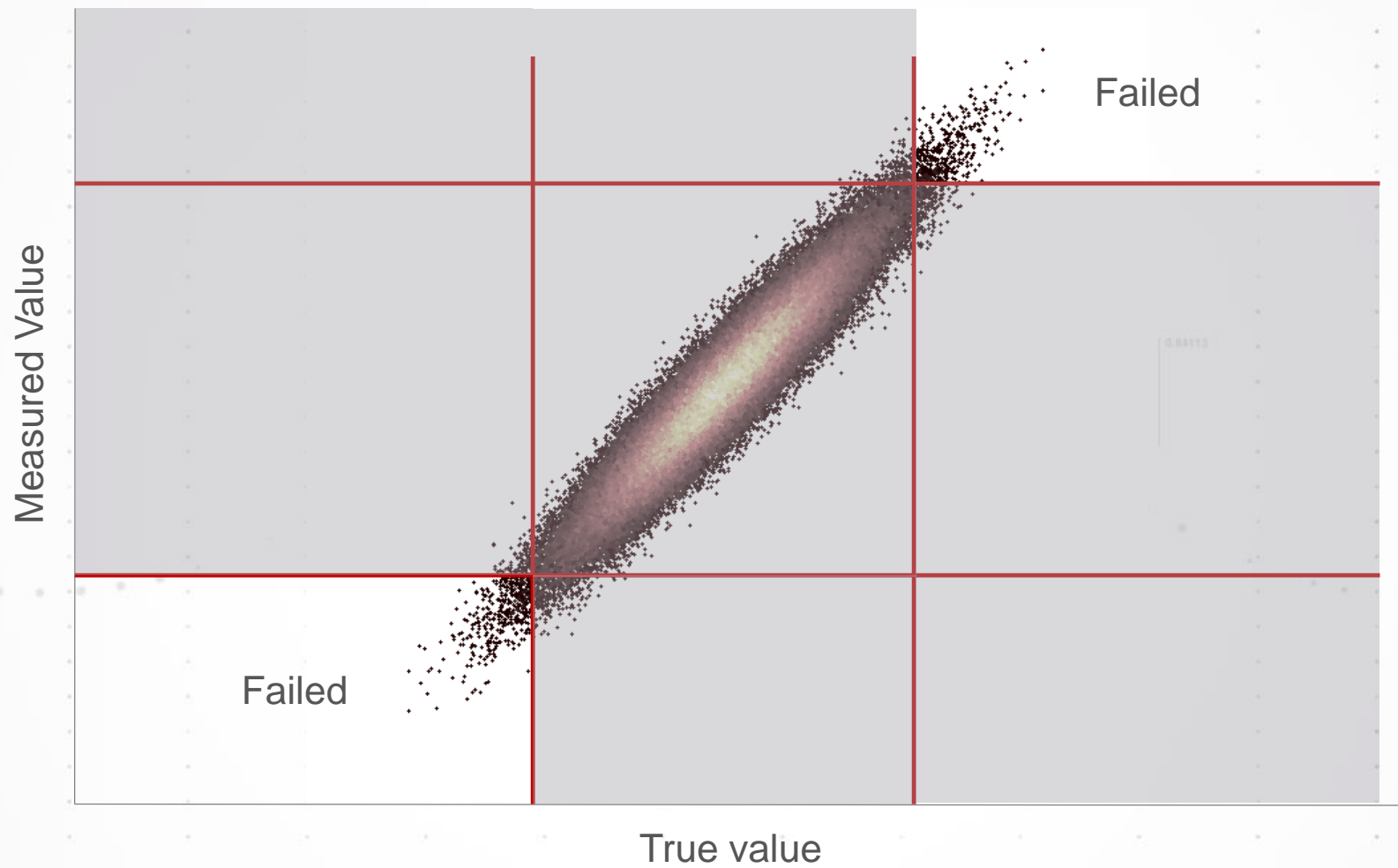


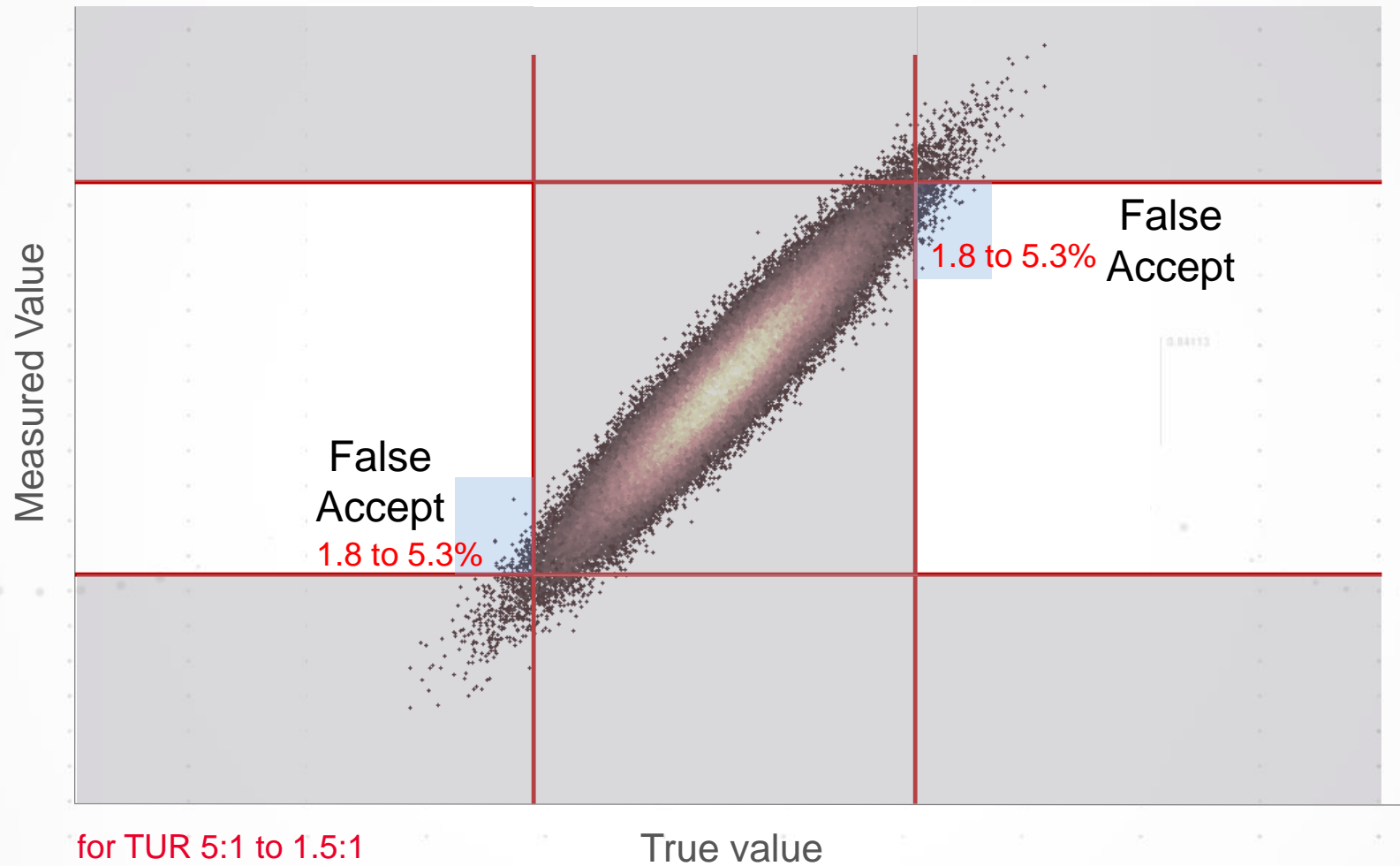


Monte Carlo simulation : [https://en.wikipedia.org/wiki/Monte\\_Carlo\\_method](https://en.wikipedia.org/wiki/Monte_Carlo_method)

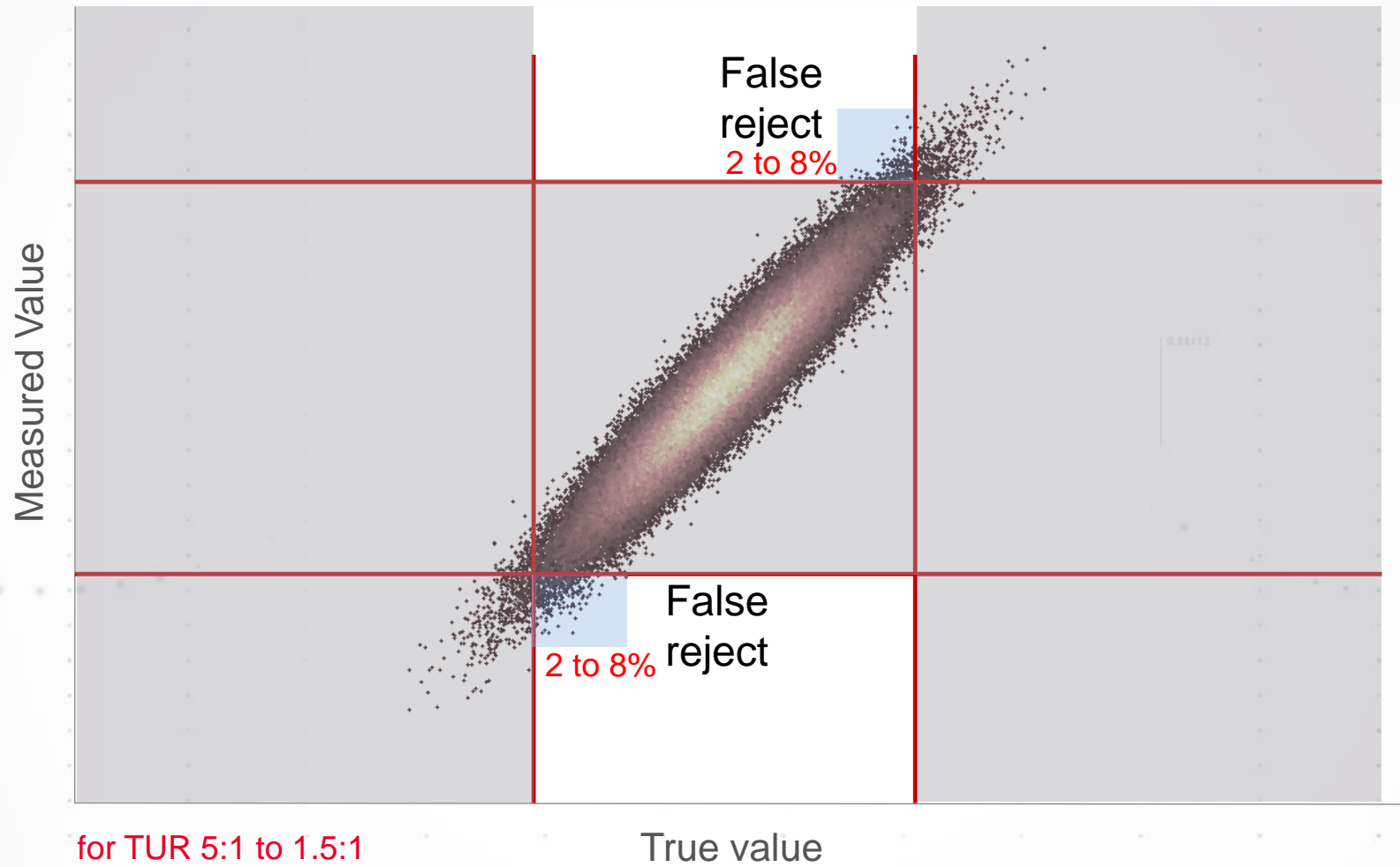








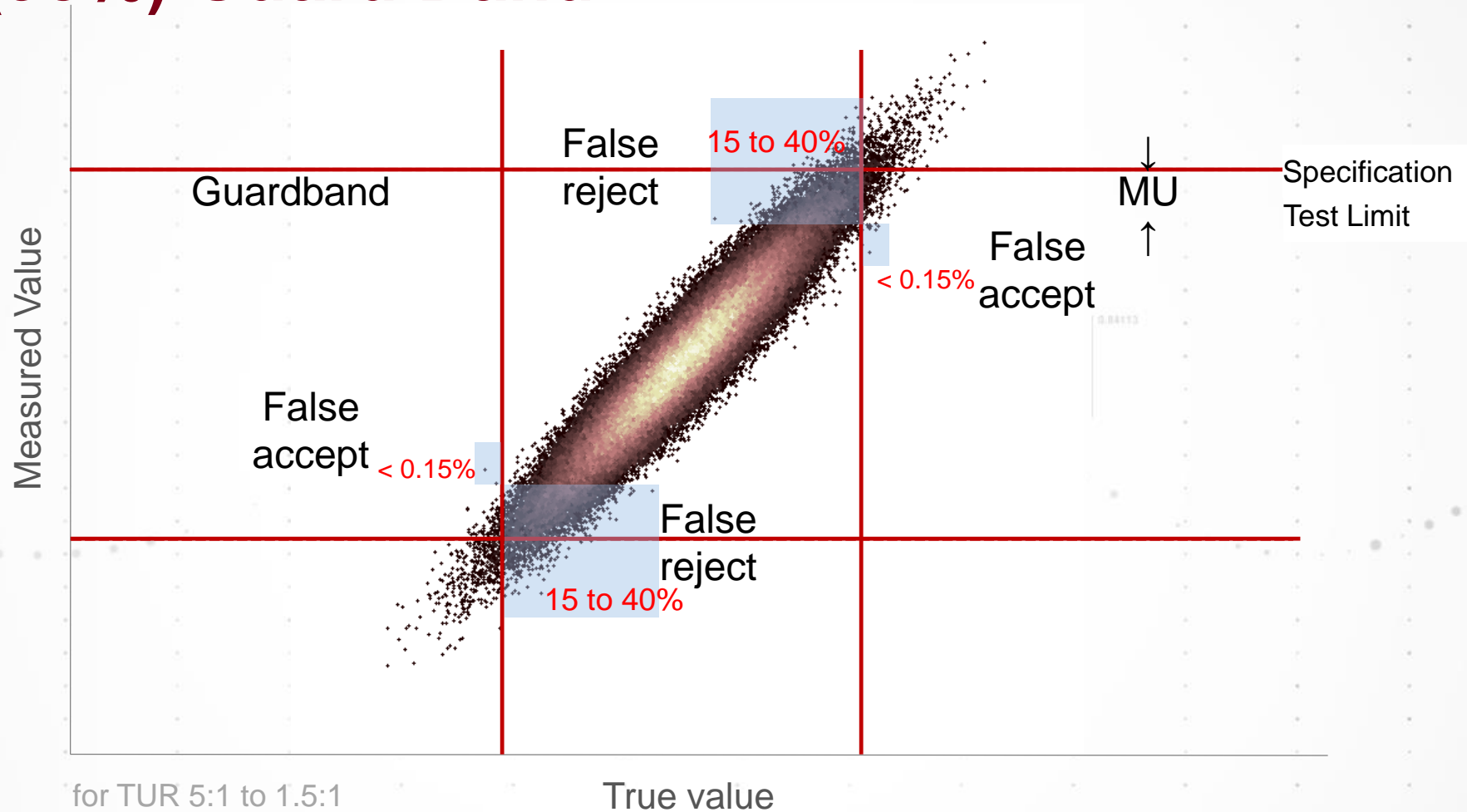
Source: Jon Harben, Senior Metrologist, Keysight Technologies



for TUR 5:1 to 1.5:1

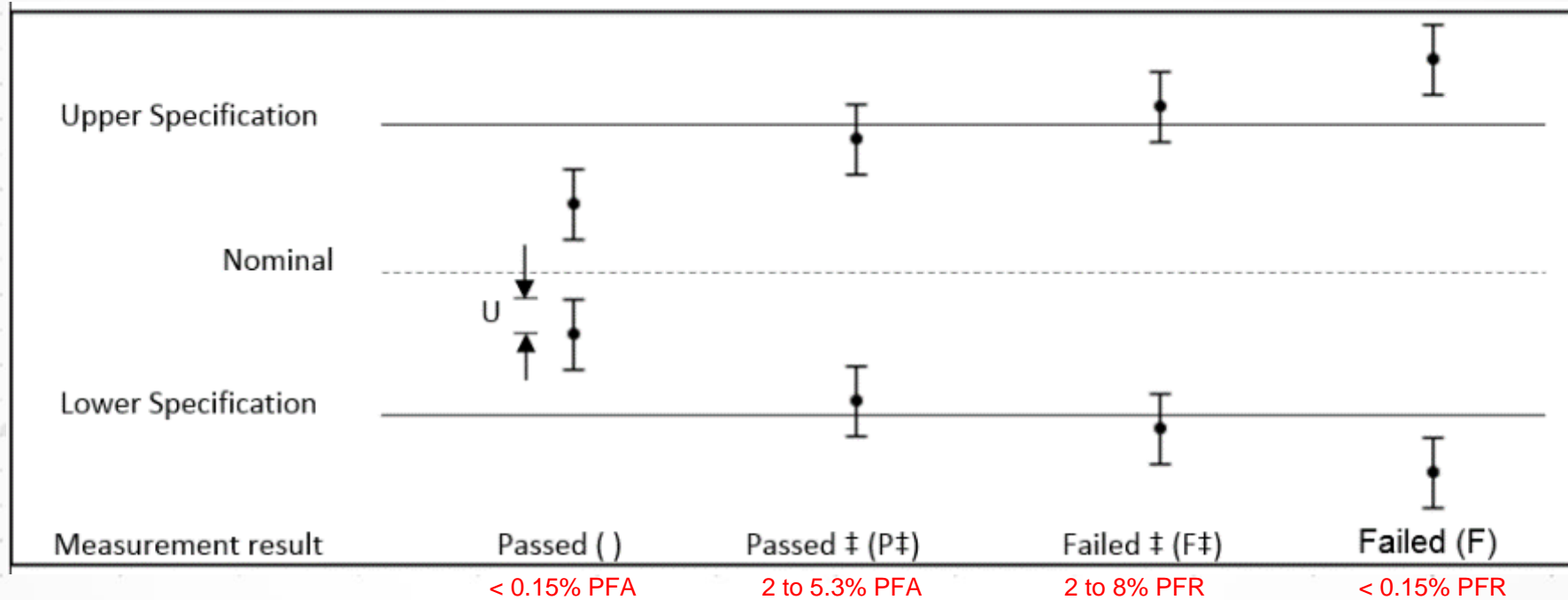
Source: Jon Harben, Senior Metrologist, Keysight Technologies

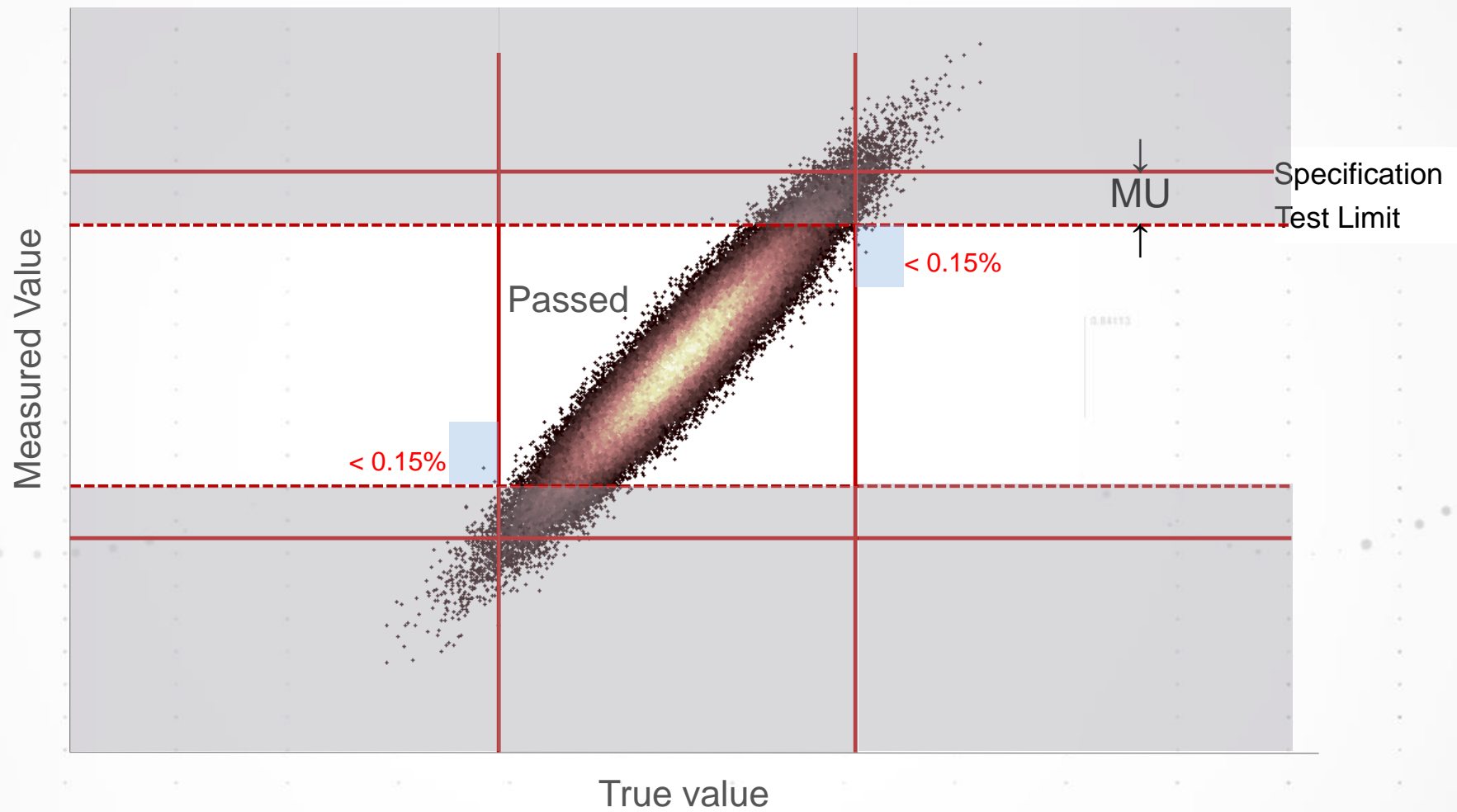
## 2 Sigma (95%) Guard Band

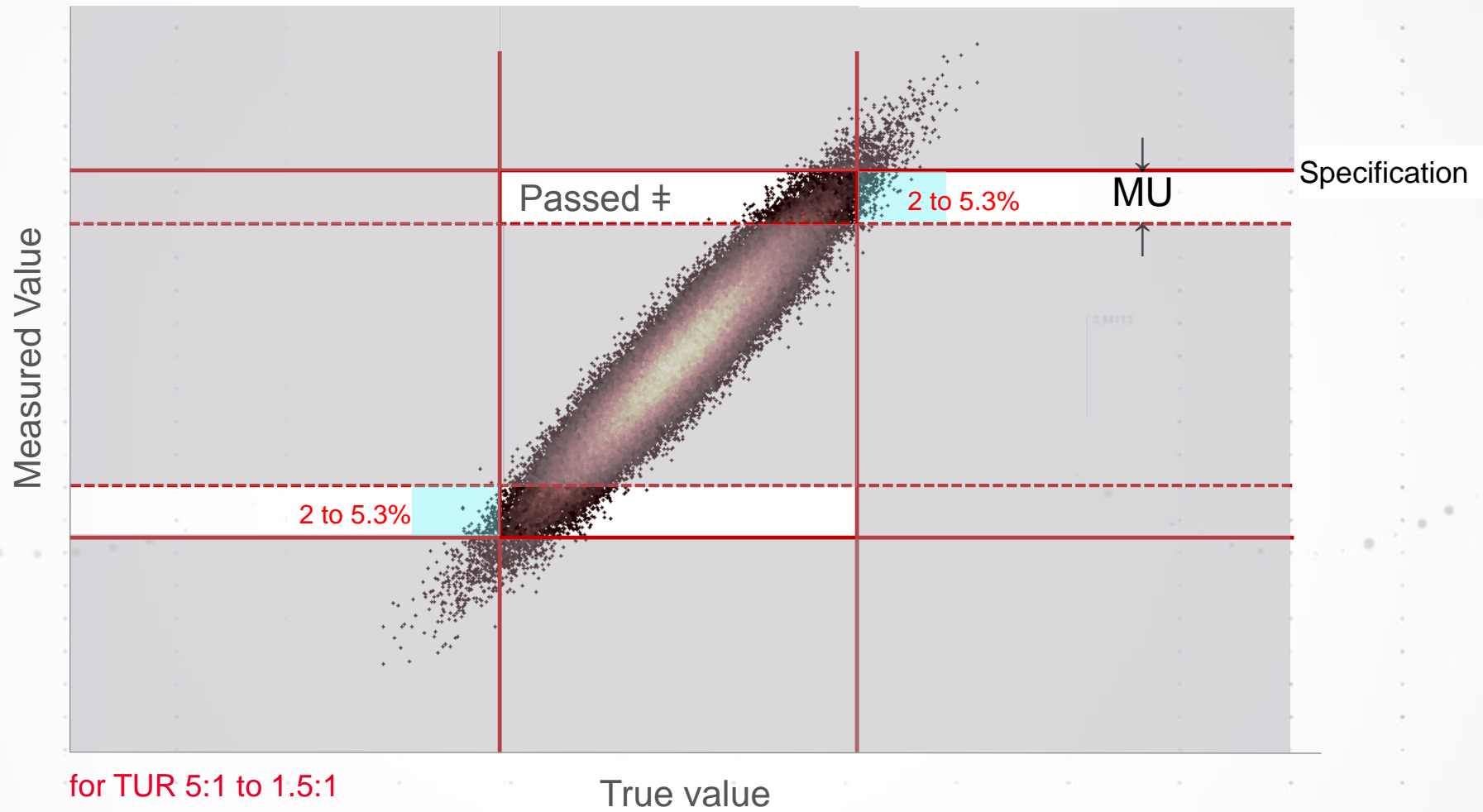


Source: Jon Harben, Senior Metrologist, Keysight Technologies

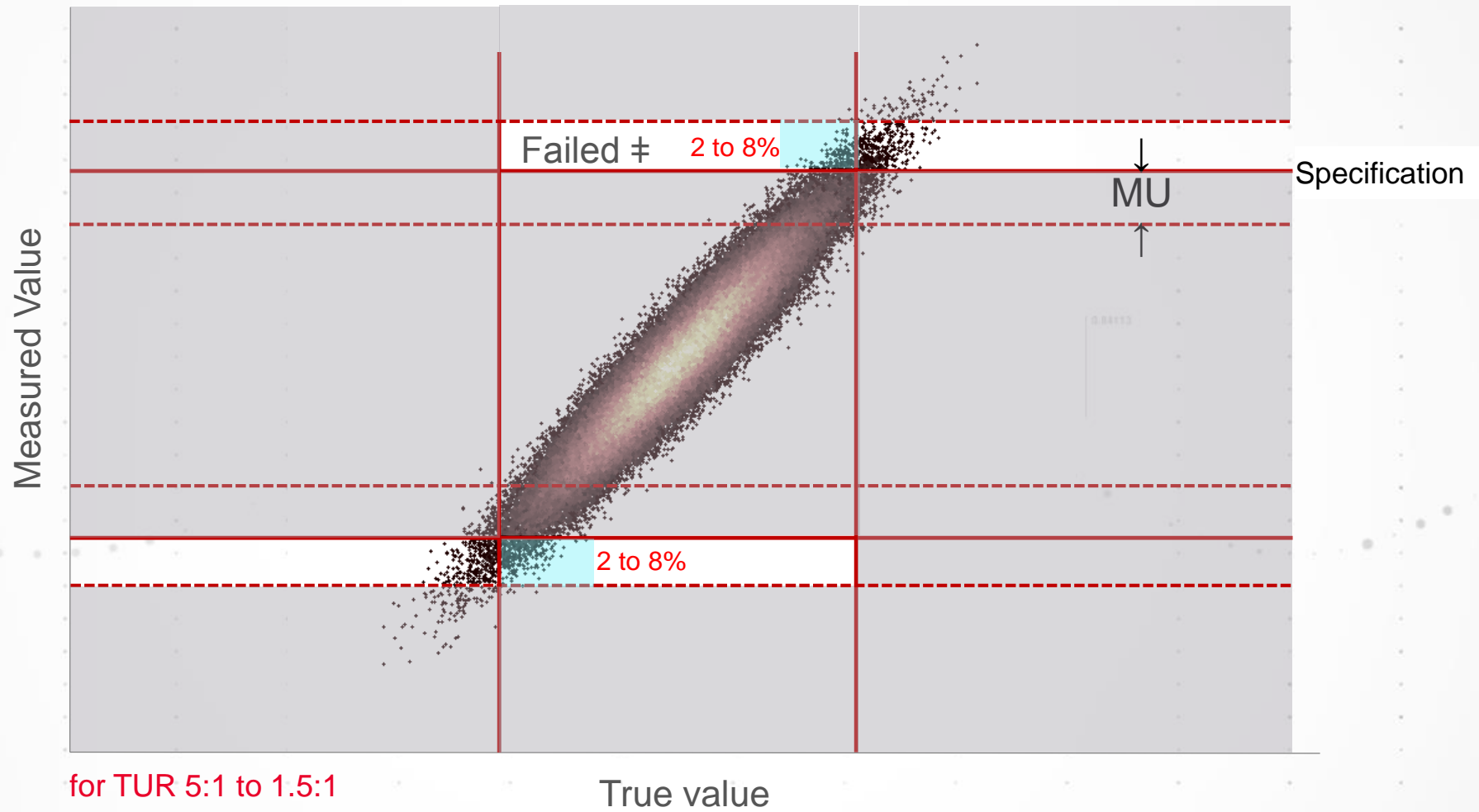
# Alternative Pass/Fail labels





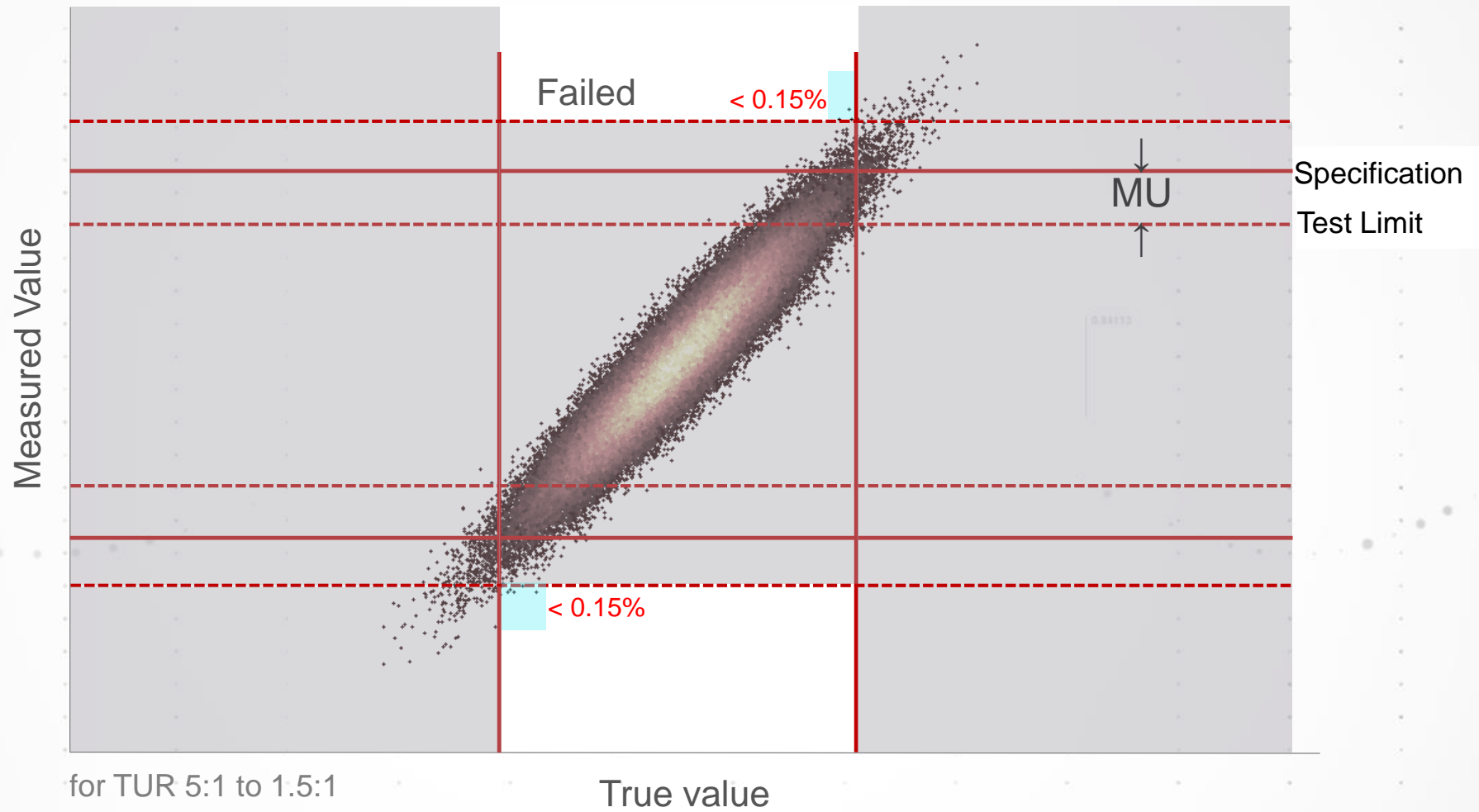


Source: Jon Harben, Senior Metrologist, Keysight Technologies



Source: Jon Harben, Senior Metrologist, Keysight Technologies





Source: Jon Harben, Senior Metrologist, Keysight Technologies

# Tool to estimate Average risk



Maximum Global Risk					
TUR <sup>1</sup>	Passed $\pm$ PFA	Failed $\pm$ PFR			
1	7.50%	13.80%			
1.25	6.10%	10.30%			
1.5	5.30%	8.10%			
1.75	4.60%	6.70%			
2	4.10%	5.70%			
2.25	3.70%	5.00%			
2.5	3.40%	4.40%			
2.75	3.10%	4.00%			
3	2.90%	3.60%			
3.25	2.70%	3.30%			
3.5	2.50%	3.00%			
3.75	2.40%	2.80%			
4	2.20%	2.60%			
4.25	2.10%	2.40%			
4.5	2.00%	2.30%			
4.75	1.90%	2.20%			
5	1.80%	2.10%			

1. TUR is Tolerance (specification) divided by measurement uncertainty.

Source: Stern & Harben, NCSLI paper 2017

# Agenda – what's next?

- What is measurement decision risk?
- Errors due to measurement decision risk
- Measurement Uncertainty (a.k.a system accuracy)
- Specific risk
- Average risk
- ➔ • Optimizing challenge: false accept vs. false reject risk.

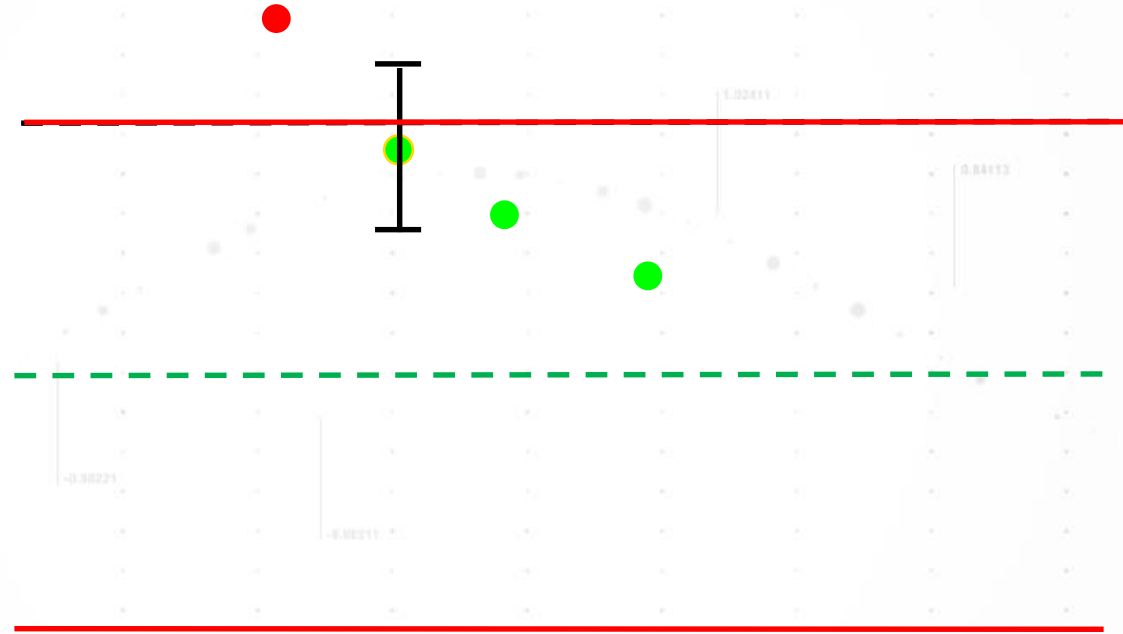
# Guard Band Drives Both False Accept & False Rejects.



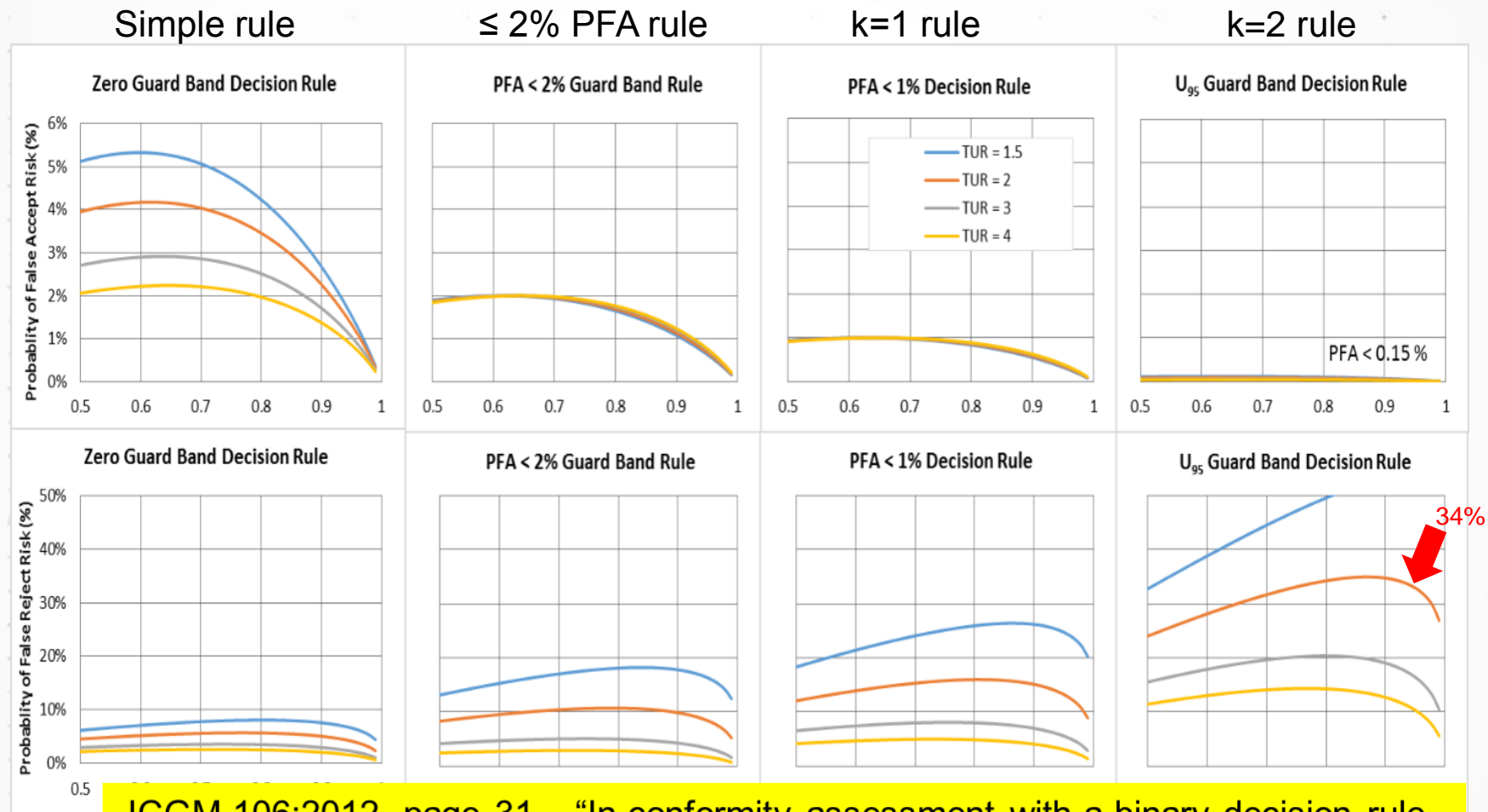
Upper specification

Nominal

Lower specification




# Average risk comparison - 4 decision rules



JCGM 106:2012, page 31 – “In conformity assessment with a binary decision rule, acting to reduce the consumer’s risk will always increase the producer’s risk.”

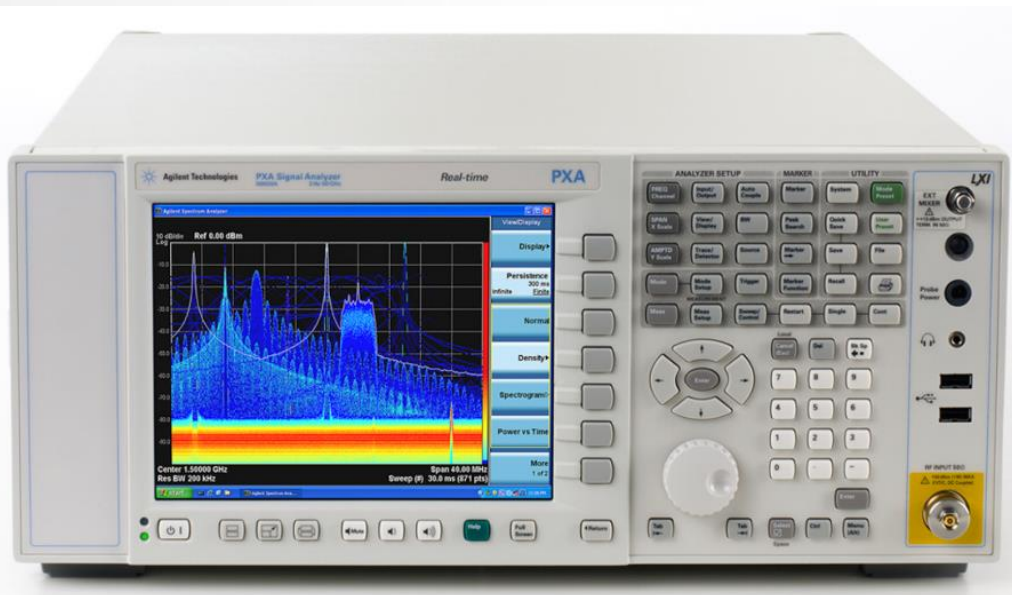
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- Optimizing challenge: false accept vs. false reject risk
- ➔ •  *“Is there any way to improve both false accept & false reject at the same time?”*



# Question

WANT TO LOWER YOUR MEASUREMENT PROCESS UNCERTAINTY?



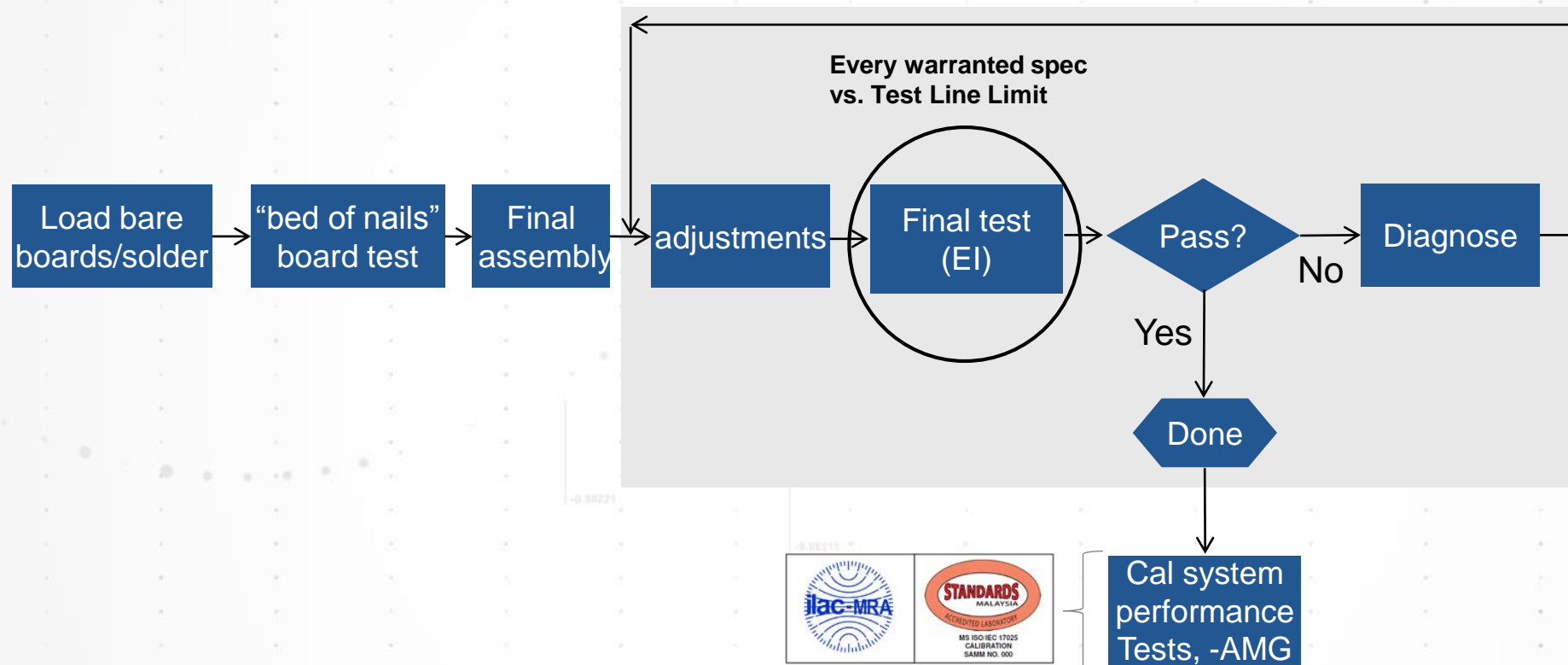
Instrument



Calibration

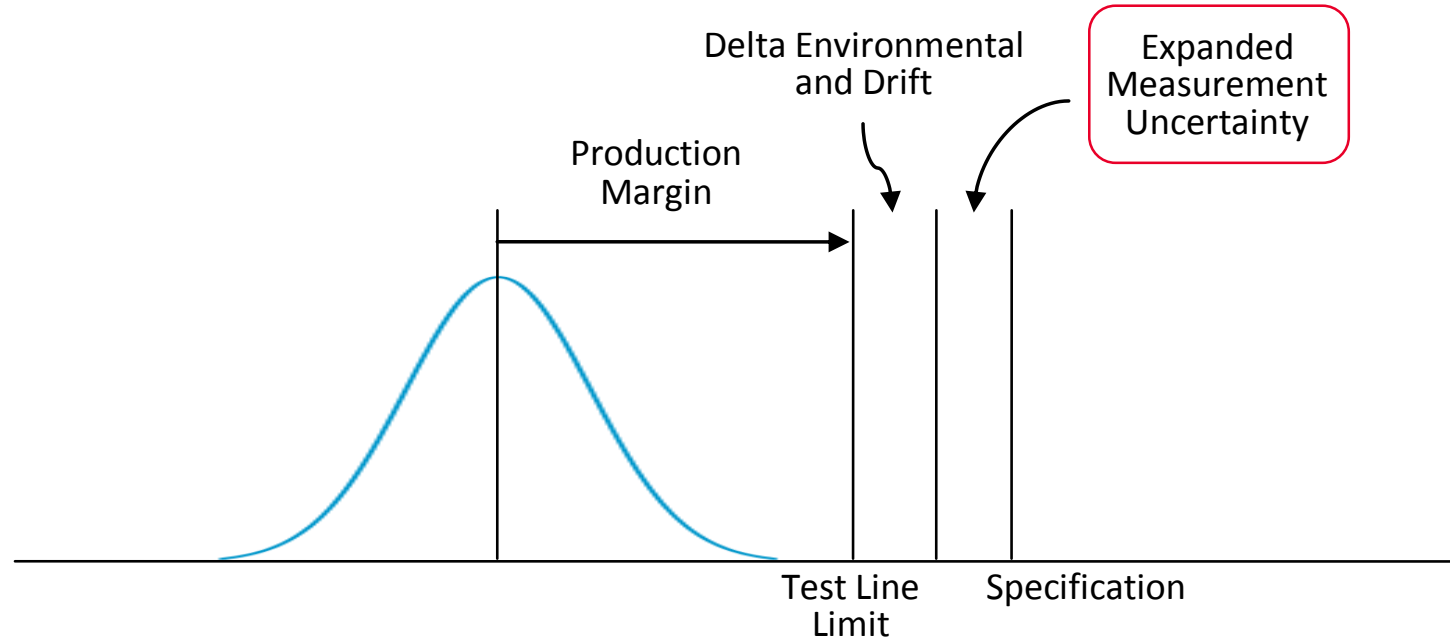
Let Keysight help you reduce your measurement uncertainty

# Factory Instrument Production Process Flow & Calibration



Courtesy of Ed Dempsey, Santa Rosa. "EI" is electronic inspection

# Meeting Specifications - Keysight Technologies



New instruments from the factory comply with ISO/IEC 17025, ILAC-G8, and ANSI/NCSL Z540.3-2006

Source: Setting and Using Specifications, Michael Dobbert, Sept 2010 issue, Measure Magazine

# Why Test Phase Noise During Calibration?



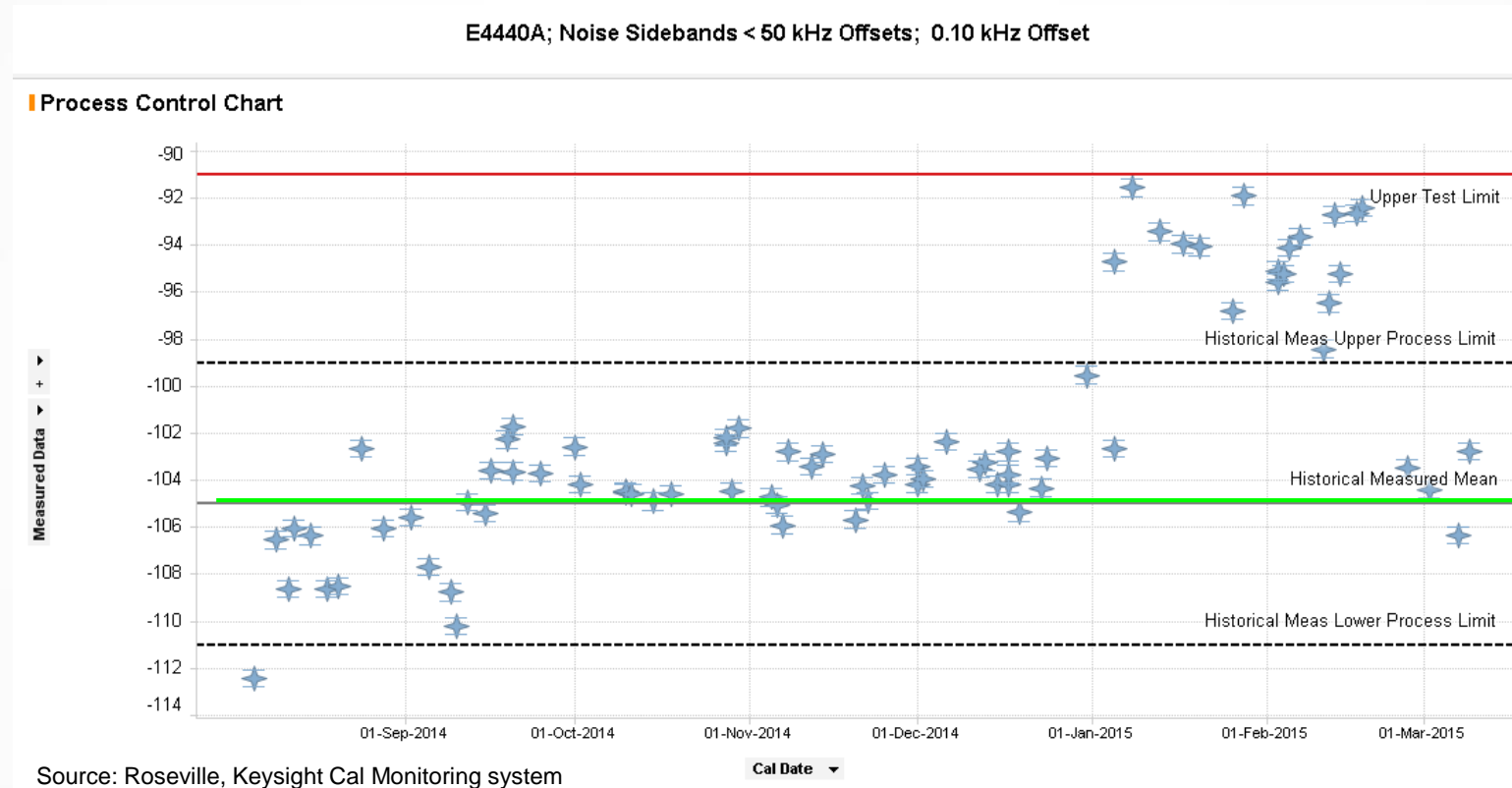
Does it really matter to test phase noise during calibration every time? My TPM tells me that *“phase noise doesn’t drift; it is part of the design.”*

**Yes it matters!**

*“Like many instrument characteristics, it doesn’t change . . . until it does!”*

# Instruments Don't Change . . . Until They Do!

Sudden phase noise measurement shift on a Spectrum Analyzer test station

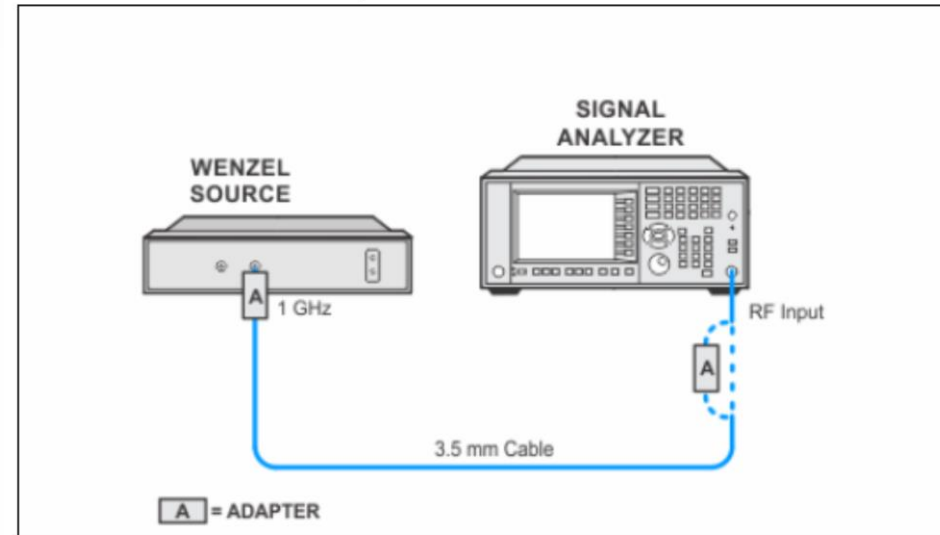


**11 dB shift!!** → the microwave signal generator that changed was in a rack, was not moved, and not power cycled.

# PXA (N9030B)/UXA (N9040B)

## HOW PHASE NOISE IS CHECKED

Phase Noise Wenzel Test Setup



### Required Test Equipment

Test Equipment	Model Number
Synthesized Signal Source	<b>Recommended model:</b> <u>Wenzel model 500-13438 Rev D</u>  <b>Alternate model for all X-Series analyzers EXCEPT UXA:<sup>1</sup></b> Wenzel model 500-13438 Rev C



# PXA (N9030B) Cal Report Excerpt: Phase Noise

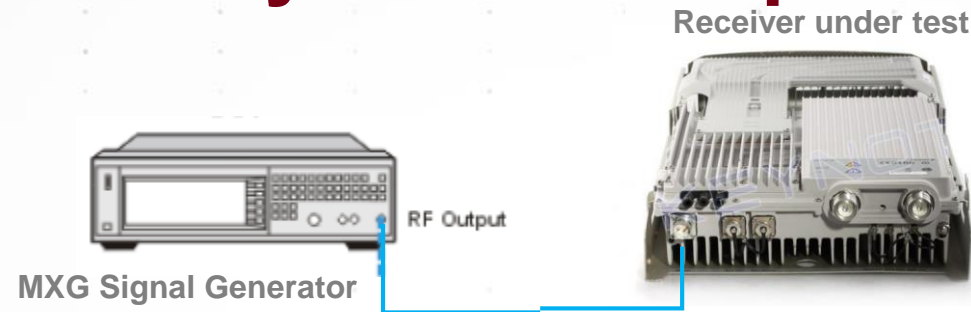
<b>Report Number</b> 1-7889090347-1-22RW		<b>Phase Noise</b>		
<b>Model</b> N9030B	<b>Serial</b> MY55520177	<b>Test Date</b> 31-May-2016	<b>Test Result</b> Passed	
<b>Environmental Conditions</b>				
<b>Temperature</b> 23.00 Celsius	<b>Humidity</b> 35.00 %	<b>Line Frequency</b> 60.00 Hz		
<b>Test Standards and Required Equipment</b>				
<b>Model</b>	<b>Description</b>	<b>Equipment ID</b>	<b>Trace Number</b>	<b>Cal Due</b>
500-13438D	Ultra Low Phase Noise Source	7243-1449	500-1343831449	14-Dec-2016
909D	50 Ohm Terminator	NONE		Cal Not Required
<b>CW Frequency = 1.00 GHz</b>				
<b>Phase Noise Offset (kHz)</b>	<b>Measured Phase Noise (dBc/Hz)</b>	<b>Specification (dBc/Hz)</b>	<b>Status</b>	
0.10	-105.10	-94.00		
0.99	-126.89	-121.00		
10.00	-136.24	-129.00		
30.00	-138.35	-130.00		
100.00	-142.44	-129.00		
1,000.00	-148.19	-145.00		
9,900.00	-156.41	-155.00		

Note: The UXA (N9040B) also has great phase noise and requires a test during calibration.

# Agenda – what's next?

- What is measurement decision risk?
- Errors due to measurement decision risk
- Measurement Uncertainty (a.k.a system accuracy)
- Specific risk
- Average risk
- Optimizing challenge: false accept vs. false reject risk
- *“Is there any way to improve both false accept and false reject?”*
- ➔ • Importance of verifying (Low level) Power Level Accuracy of signal generators

# Receiver Sensitivity Test Example

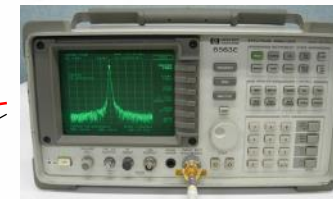


## How measured:

Find the minimum RF signal level needed to produce minimum intelligible communication [target (S+N)/N or BER]. [Iterative process]

## Test Conditions:

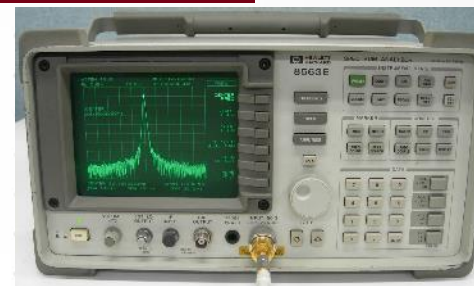
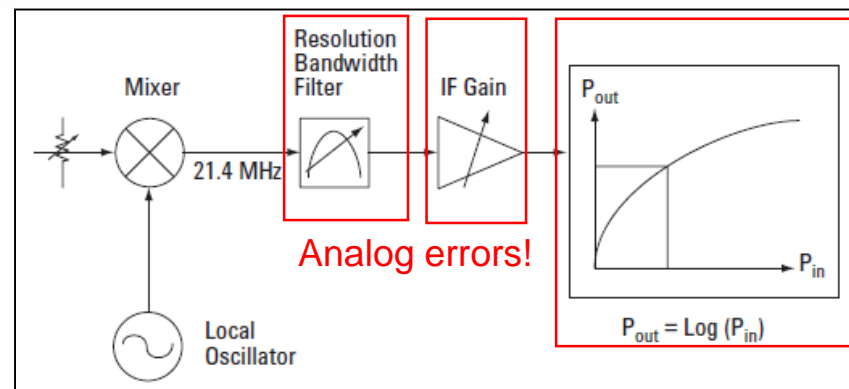
- 107 dBm (1.0  $\mu$ V) Customer spec.
  - 
  - $>\pm 1.5$  dB MU
  - $\pm 0.2$  dB MU
- Case 1: MXG calibrated w/8563E (3<sup>rd</sup> party)
- Case 2: MXG calibrated w/E4448A (Keysight)



# Key Test Standards

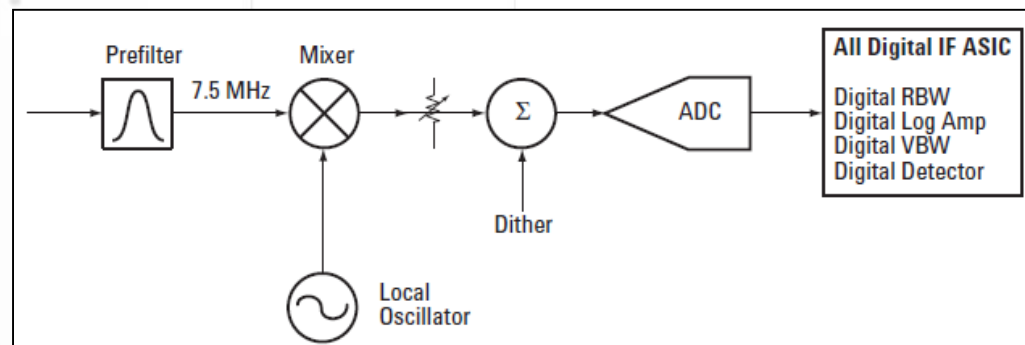
## SIGNAL GENERATOR LOW LEVEL POWER ACCURACY TEST

$>\pm 1.5$  db error at  
-107 dBm



Traditional analog IF  
Section, i.e. **8563E**

$<\pm 0.2$  db  
error at -107  
dBm



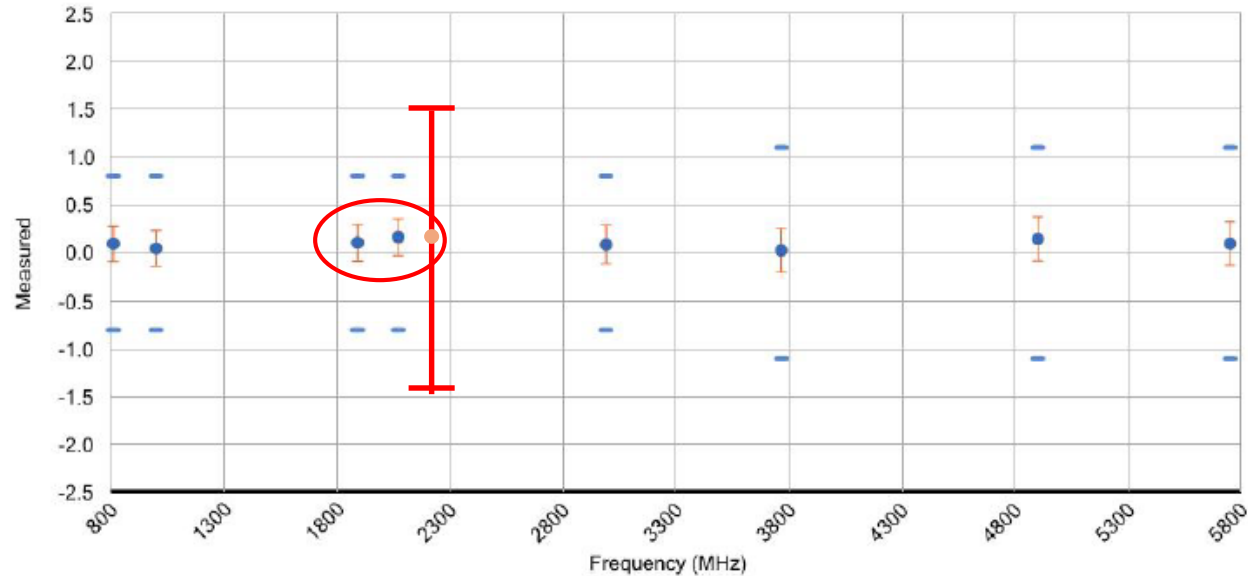
All-digital IF Section  
**E444xA**

# Typical MXG Cal Result at -110 dBm



## Power Level Accuracy (cont.)

Test Power = -110.00 dBm, Digital



Test Power = -110.00 dBm, Digital

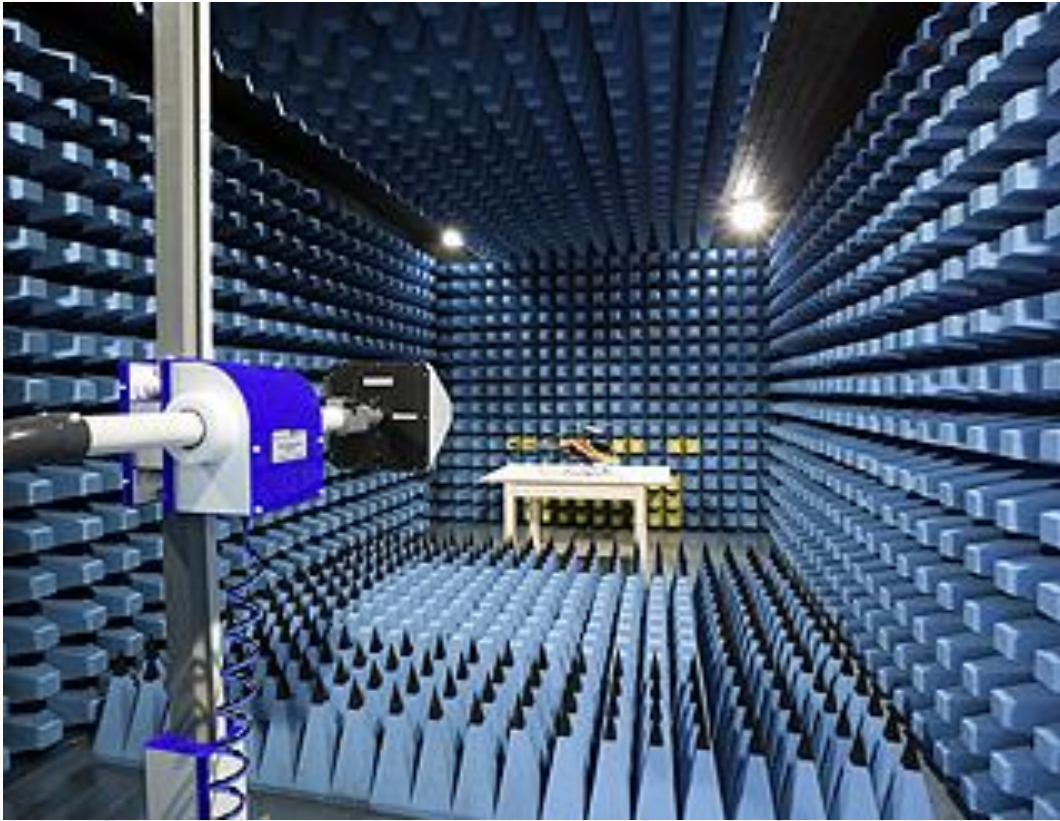
Frequency	Minimum	Measured	Maximum	Uncertainty	Status
810.001 MHz	-0.8 dB	0.09 dB	0.8 dB	0.18 dB	
999.001 MHz	-0.8 dB	0.04 dB	0.8 dB	0.19 dB	
1890.001 MHz	-0.8 dB	0.10 dB	0.8 dB	0.19 dB	
2070.001 MHz	-0.8 dB	0.16 dB	0.8 dB	0.19 dB	

# Decision Rule Examples



## Example 2: New Prototype Sent to a Test Lab for Assessing Compliance to CISPR 16

Which Decision Rule/amount of guard band is most appropriate??

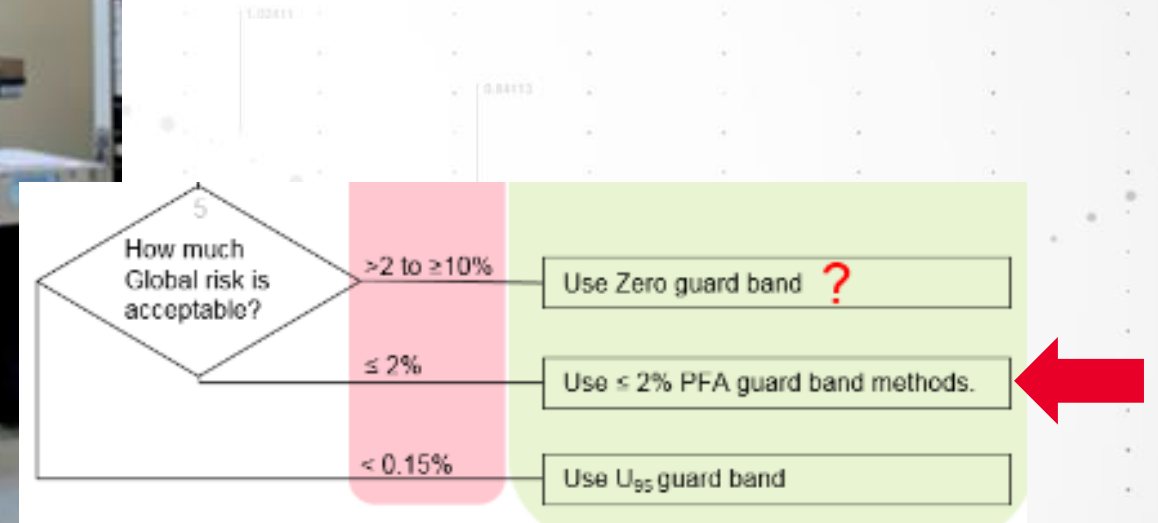


 No population exists, so recommend guard band of  $U_{95}$  (Specific risk)

# Example 3: Production Instrument Submitted for Periodic Calibration



End customer wants a [binary] Pass or Fail statement of conformance to specification.



# Conclusions/Call-to-Action

1. All measurements contain errors 🤖
2. Estimate your system accuracy (measurement uncertainty)
3. Determine the maximum % False pass/False reject risks you can tolerate.
4. Select a decision rule with suitable guard band to achieve your % risk tolerance.
5. Minimize instrument [drift] error contributions with regular [accurate] calibration.



# YouTube Videos for More Information

- What calibration is supposed to do
- What service deliverables you should receive
- How to get measurement uncertainties for your instrument's current performance

<https://www.youtube.com/playlist?list=PLvQ5Bzr3tM50No0sfwYr40jA50rsIQyD->